Sorting M269 Tutorial Prsntn 2025J

Phil Molyneux

4 January 2026

Sorting

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Agenda

Adobe Connect

Sorting: Motivation

Sorting Taxonomy

Recursion/Iteration

Split/Join Sorting Non-Comparison

Sorts Future Work

D - f - - - - - -

M269 Tutorial: Sorting, Recursion

Agenda

Welcome & introductions

Tutorial topics: Sorting Algorithms, Recursion

 Adobe Connect — if you or I get cut off, wait till we reconnect (or send you an email)

Time: about 1.5 hours

Do ask questions or raise points.

Source: of slides, notes, programs and playing cards: M269Tutorial20250105SortingPrsntn2024J/ Sorting

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References

www.pmolyneux.co.uk/OU/M269FolderSync/M269TutorialNotes/M269Tutorial20250105SortingPrsntn2024J/

M269 Tutorial

Introductions — Phil

- Name Phil Molyneux
- Background
 - Undergraduate: Physics and Maths (Sussex)
 - Postgraduate: Physics (Sussex), Operational Research (Brunel), Computer Science (University College, London)
 - Worked in Operational Research, Business IT, Web technologies, Functional Programming
- First programming languages Fortran, BASIC, Pascal
- Favourite Software
 - ► Haskell pure functional programming language
 - ► Text editors TextMate, Sublime Text previously Emacs
 - ▶ Word processing in MTFX all these slides and notes
 - Mac OS X
- Learning style I read the manual before using the software

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- ► Name?
- Favourite software/Programming language?
- Favourite text editor or integrated development environment (IDE)
- List of text editors, Comparison of text editors and Comparison of integrated development environments
- Other OU courses?
- Anything else?

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Sorting: Motivation

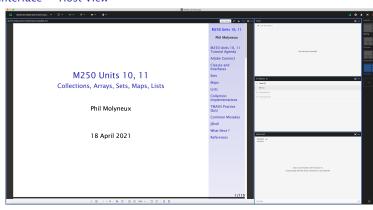
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Interface — Host View



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Interface

Settings Sharing Screen & Applications Ending a Meeting

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Chat Pods Web Graphics Recordings

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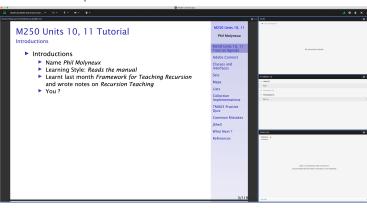
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Interface — Participant View



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Settings

- Everybody Menu bar Meeting Speaker & Microphone Setup
- Menu bar Microphone Allow Participants to Use Microphone
- Check Participants see the entire slide Workaround
 - Disable Draw Share pod Menu bar Draw icon
 - Fit Width Share pod Bottom bar Fit Width icon
- Meeting Preferences General Host Cursor Show to all attendees
- Menu bar Video Enable Webcam for Participants
- Do not Enable single speaker mode
- Cancel hand tool
- Do not enable green pointer
- Recording Meeting Record Session
- Documents Upload PDF with drag and drop to share pod
- ► Delete <u>Meeting</u> <u>Manage Meeting Information</u> <u>Uploaded Content</u> and <u>check filename</u> <u>click on delete</u>

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Access

Tutor Access

TutorHome M269 Website Tutorials Cluster Tutorials M269 Online tutorial room Tutor Groups M269 Online tutor group room Module-wide Tutorials M269 Online module-wide room

Attendance

TutorHome Students View your tutorial timetables

- Beamer Slide Scaling 440% (422 x 563 mm)
- Clear Everyone's Status

Attendee Pod Menu Clear Everyone's Status

Grant Access and send link via email Meeting Manage Access & Entry Invite Participants...

Presenter Only Area

Meeting Enable/Disable Presenter Only Area

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Keystroke Shortcuts

- Keyboard shortcuts in Adobe Connect
- ► Toggle Mic 🖁 + M (Mac), Ctrl + M (Win) (On/Disconnect)
- ► Toggle Raise-Hand status 🗯 + 🗉
- ► Close dialog box 🔊 (Mac), Esc (Win)
- ► End meeting #+\

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- Share menu Change View Zoom in for mismatch of screen size/resolution (Participants)
- ► (Presenter) Change to 75% and back to 100% (solves participants with smaller screen image overlap)
- Leave the application on the original display
- Beware blued hatched rectangles from other (hidden) windows or contextual menus
- Presenter screen pointer affects viewer display beware of moving the pointer away from the application
- First time: System Preferences Security & Privacy Privacy Accessibility

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Ending a Meeting

- Notes for the tutor only
- ► Student: Meeting Exit Adobe Connect
- ► Tutor:
- ► Recording Meeting Stop Recording ✓
- Remove Participants Meeting End Meeting...
 - Dialog box allows for message with default message:
 - The host has ended this meeting. Thank you for attending.
- Recording availability In course Web site for joining the room, click on the eye icon in the list of recordings under your recording — edit description and name
- ► Meeting Information Meeting Manage Meeting Information can access a range of information in Web page.
- Delete File Upload Meeting Manage Meeting Information
 Uploaded Content tab select file(s) and click Delete
- Attendance Report see course Web site for joining room

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Invite Attendees

Provide Meeting URL Menu Meeting Manage Access & Entry Invite Participants...

- ► Allow Access without Dialog Menu Meeting

 Manage Meeting Information provides new browser window with Meeting Information Tab bar Edit Information
- Check Anyone who has the URL for the meeting can enter the room
- ▶ Default Only registered users and accepted guests may enter the room
- Reverts to default next session but URL is fixed
- Guests have blue icon top, registered participants have yellow icon top — same icon if URL is open
- ► See Start, attend, and manage Adobe Connect meetings and sessions

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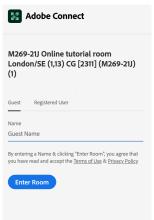
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Future Work

Entering a Room as a Guest (1)

- Click on the link sent in email from the Host
- Get the following on a Web page
- As Guest enter your name and click on Enter Room



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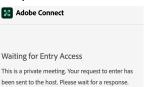
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Entering a Room as a Guest (2)

See the Waiting for Entry Access for Host to give permission



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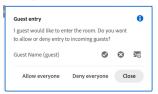
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Entering a Room as a Guest (3)

Host sees the following dialog in Adobe Connect and grants access



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Layouts

- Creating new layouts example Sharing layout
- Menu Layouts Create New Layout... Create a New Layout dialog

 Create a new blank layout and name it PMolyMain
- New layout has no Pods but does have Layouts Bar open (see Layouts menu)
- Pods
- Menu Pods Share Add New Share and resize/position initial name is Share n— rename PMolyShare
- Rename Pod Menu Pods Manage Pods... Manage Pods Select Rename or Double-click & rename
- Add Video pod and resize/reposition
- Add Attendance pod and resize/reposition
- ► Add Chat pod rename it *PMolyChat* and resize/reposition

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Chat Pods

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Layouts

- Dimensions of Sharing layout (on 27-inch iMac)
 - Width of Video, Attendees, Chat column 14 cm
 - ► Height of Video pod 9 cm
 - ► Height of Attendees pod 12 cm
 - Height of Chat pod 8 cm
- ► **Duplicating Layouts** does *not* give new instances of the Pods and is probably not a good idea (apart from local use to avoid delay in reloading Pods)
- Auxiliary Layouts name PMolyAuxOn
 - Create new Share pod
 - Use existing Chat pod
 - Use same Video and Attendance pods

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Chat Pods

- Format Chat text
- Chat Pod menu icon My Chat Color
- Choices: Red, Orange, Green, Brown, Purple, Pink, Blue, Black
- Note: Color reverts to Black if you switch layouts
- Chat Pod menu icon Show Timestamps

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Graphics Conversion

PDF to PNG/JPG

- Conversion of the screen snaps for the installation of Anaconda on 1 May 2020
- Using GraphicConverter 11
- File Convert & Modify Conversion Convert
- Select files to convert and destination folder
- ► Click on Start selected Function or 🖁 + 🗇

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Exporting Recordings

- Menu bar Meeting Preferences Video
- Aspect ratio Standard (4:3) (not Wide screen (16:9) default)
- ► Video quality Full HD (1080p not High default 480p)
- ► Recording Menu bar Meeting Record Session ✓
- Export Recording
- Menu bar Meeting Manage Meeting Information
- New window Recordings check Tutorial Access Type button
- check Public check Allow viewers to download
- Download Recording
- New window Recordings check Tutorial Actions Download File

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Sorting

Motivation

- Motivation for studying sorting algorithms
- ► Taxonomy of sorting see Wikipedia Sorting Algorithm
- Abstract comparison sort split/join algorithm
- Insertion sort and selection sort described with split/join algorithm diagram and implemented in Python. (A previous edition also included optional Haskell code)
- Recursive and iterative versions
- Mergesort, Quicksort and Bubble sort in the same framework
- Sorting via a data structure Tree sort
- Comparison sorts and Distribution sorts
- Review of Web sites and sorting algorithms used in practice

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Future Work

- ... virtually every important aspect of programming arises somewhere in the context of sorting or searching.
- How are good algorithms discovered?
- How can given algorithms and programs be improved?
- How can the efficiency of algorithms be analyzed mathematically?
- How can a person choose rationally between different algorithms for the same task?
- In what senses can algorithms be proved best possible?
- How does the theory of computing interact with practical considerations?

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Sorting Algorithms

Demonstration 1 Sorting Algorithms as Dances

- AlgoRythmics
- Videos tab Insertion Sort
- Insertion Sort
- This is the Romanian folk music that inspired Bartók
- Compare the dance with the Python algorithm for Insertion Sort below

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- Almost everyone has played cards and, as part of any card game, will have sorted cards in their hand
- This exercise is aimed at writing down how you sort you cards and giving these instructions to another person to follow.
- Decide on your general ordering of playing cards you are free to set any ordering you like but here is the usual ordering for suits and values:

```
Clubs < Diamonds < Hearts < Spades

Two < Three < Four < Five < Six
< Seven < Eight < Nine < Ten
< Jack < Queen < King < Ace
```

Write down your method for sorting cards — the method must specify how to choose a card to move and where to move it to. Agenda

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- Using your method, sort the cards record the order of the cards after each move of a card
- Now swap your written method and the cards in your original order with another student.
- Follow the other student's method to sort the cards and record your steps

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Activity 1 Card Sorting Exercise

Working Space

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ruture work

Activity 1 Card Sorting Exercise (3)

Discussion

- Did both of you end up with the same sequence of steps?
- Did any of the instructions require human knowledge?
- General point: probably most people use some variation on *Insertion sort* or *Selection sort* but would have steps that had multiple shifts of cards.
- Note: This activity may be done on the Whiteboard using cards from http://pmolyneux.co.uk/OU/M269/ M269TutorialNotes/M269TutorialSorting/Cards/

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Taxonomy of Sorting Algorithms

Comparison Sorts

- Computational complexity worst, best, average number of comparisons, exchanges and other program contructs (but see http://www.softpanorama.org/ Algorithms/sorting.shtml for Slightly Skeptical View) — O(n²) bad, O(nlog n) better
- Other issues: space behaviour, performance on typical data sets, exchanges versus shifts
- Abstract sorting algorithm Following Merritt (1985, 1997) and Azmoodeh (1990, chp 9), we classify the divide and conquer sorting algorithms by easy/hard split/join
- see diagram below

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Sorting Classifications

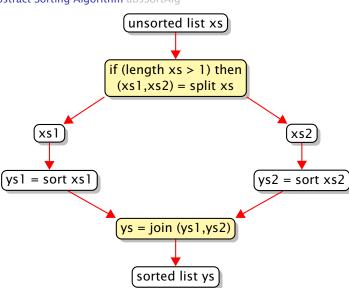
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Taxonomy of Sorting Algorithms

Abstract Sorting Algorithm absSortAlg



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Sorting Algorithms

Other Classifications

- See Wikipedia Sorting algorithm for big list
- Comparison Sorts
 - Insertion sort, Selection sort, Merge sort, Quicksort, Bubble sort
 - Sorting via a data structure: Tree sort, Heap sort
- Non-Comparison sorts distribution sorts bucket sort, radix sort
- Sorts used in Programming Language Libraries
 - Powersort and Timsort by Tim Peters used in Python and Java — combination of merge and insertion sorts
 - Haskell modified Mergesort by Ian Lynagh in GHC implementation

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- Many functions are naturally defined using recursion
- A recursive function is defined in terms of calls to itself acting on smaller problem instances along with a base case(s) that terminate the recursion
- ► Classic example: Factorial $n! = n \times (n-1) \cdots 2 \times 1$

```
5def fac(n) :
     return n * fac(n-1)
```

- We can evaluate fac(6) by using a substitution model (section 1.1.5) for function application
- To evaluate a function applied to arguments, evaluate the body of the function with each formal parameter replaced by the corresponding actual arguments. Abelson and Sussman (1996, section 1.1.5) Structure and Interpretation of Computer Programs

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| | Expression to Evaluate | Reason |
|---------------|------------------------------------|----------------|
| | fac(6) | Initial line 5 |
| \rightarrow | 6 * fac(5) | line 8 |
| \rightarrow | 6 * (5 * fac(4)) | line 8 |
| \rightarrow | 6 * (5 * (4 * fac(3)) | line 8 |
| \rightarrow | 6 * (5 * (4 * (3 * fac(2)))) | line 8 |
| \rightarrow | 6 * (5 * (4 * (3 * (2 * fac(1))))) | line 8 |
| \rightarrow | 6 * (5 * (4 * (3 * (2 * 1)))) | line 6 |
| \rightarrow | 720 | Arithmetic |

- This occupies more space in the process of evaluation since we cannot do the multiplications until we reach the base case of fac()
- This is a recursive function and a linear recursive process
- ► *Implemented* in Python (and most imperative languages) with a *stack* of function calls
- We can define an equivalent factorial function that produces a different process

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Recursion

Iterative Factorial

```
24 def facIter(n) :
25    return accProd(n,1)

27 def accProd(n,x) :
28    if n = 1 :
29     return x
30    else :
31    return accProd(n-1, n * x)
```

- facIter() uses accProd() to maintain a running product and accumulate the final result to return
- We can display the evaluation of facIter(6) using the substitution model

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Recursion

Evaluation of facIter(6)

| | Expression to Evaluate | Reason |
|---------------|------------------------|-----------------|
| | facIter(6) | Initial line 24 |
| \rightarrow | accProd(6,1) | line 25 |
| \rightarrow | accProd(5, 6 * 1) | line 30 & (*) |
| \rightarrow | accProd(4, 5 * 6) | line 30 & (*) |
| \rightarrow | accProd(3, 4 * 30) | line 30 & (*) |
| \rightarrow | accProd(2, 3 * 120) | line 30 & (*) |
| \rightarrow | accProd(1, 2 * 360) | line 30 & (*) |
| \rightarrow | 720 | line 28 & (*) |

- This occupies constant space at each stage all the variables describing the state of the calculation are in the function call
- This is a recursive program and an iterative process
- We are assuming the multiplication is evaluated at each function call (strict or eager evaluation)
- Also referred to as tail recursion we need not build a stack of calls

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Recursion and Iteration

Iterative Factorial Exercises

- Write a version of the factorial function using a while loop in Python
- Write a version of the factorial function using a for loop in Python

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Iterative Factorial Exercises — Solutions

Factorial function using a while loop in Python

Factorial function using a for loop in Python

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Tail Recursion and Iteration

- ▶ When the structured programming ideas emerged in the 1960s and 1970s the languages such as C and Pascal implemented recursion by always placing the calls on the stack — Python follows this as well
- This means that in those languages they have to have special constructs such as for loops, while loops, to express iterative processes without recursion
- A for loop is syntactically way more complicated than a recursive definition
- Some language implementations (for example, Haskell) spot tail recursion and do not build a stack of calls
- You still have to write your recursion in particular ways to allow the compiler to spot such optimisations.

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- ▶ Bohm & Jacopini (1966) showed that structured programming with a combination of sequence, selection, iteration and procedure calls was Turing complete (see Unit 7)
- In the late 1980s two books came out that were particularly influential:
- Abelson and Sussman (1984, 1996) Structure and Interpretation of Computer Programs (known as SICP) which was the programming course for the first year at MIT,
- ▶ Bird and Wadler (1988, 1998, 2014) *Introduction to Functional Programming* which was the the programming course for the first year at Oxford.
- See SICP online and Section 1.2 Procedures and the Process They Generate

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Sorts **Future Work**

References

Structured Programming, GOTO and Recursion (2)

- Dijkstra (1968) Go To Statement Considered Harmful illustrates a debate on structured programming
- ► The von Neumann computer architecture takes the memory and state view of computation as in Turing m/c
- Lambda calculus is equivalent in computational power to a Turing machine (Turing showed this in 1930s) but efficient implementations did not arrive until 1980s
- Functional programming in Lisp or APL was slow
- Alan Perlis (1982) Epigrams on Programming: [Functional programmers] know the value of everything but the cost on nothing
- Erik Meijer (1991) Recursion is the GOTO of functional programming
- Leading to common patterns of higher order functions, map, filter, fold and polymorphic data types

Split/Join Sorting Algorithms

Example Algorithms & Implementation

- Insertion Sort
- Selection Sort
- ► Merge Sort
- Quicksort
- Bubble Sort
- Implementations in Python, recursive and non-recursive

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Split/Join Sorting

Insertion Sort Selection Sort Merge Sort Quicksort Bubble Sort

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Abstract Algorithm

- Insertion Split xs1 is the singleton list of the first item; xs2 is the rest of the list
- Insertion Join insert the item in the singleton list into the sorted result of the rest of the list

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Split/Join Sorting

Insertion Sort —

Abstract Algorithm
Insertion Sort — Python

Activity 2 — Insertion Sort: Trace an Evaluation

Insertion Sort — Non-recursive Activity 3 — Insertion Sort Non-recursive

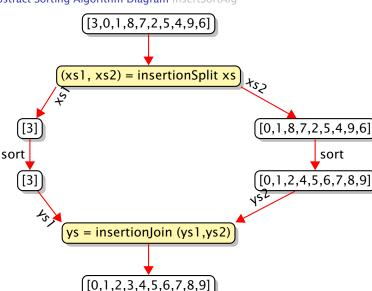
Trace Selection Sort Merge Sort

Quicksort Bubble Sort

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Abstract Sorting Algorithm Diagram insertSortAlg



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> Insertion Sort — Abstract Algorithm

Insertion Sort — Python Activity 2 — Insertion Sort: Trace an Evaluation

Insertion Sort —
Non-recursive
Activity 3 — Insertion

Sort Non-recursive Trace Selection Sort

Merge Sort Quicksort Bubble Sort

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Python Implementation

```
4def insSort(xs) :
    if len(xs) \ll 1:
      return xs
    else:
      return ins(xs[0],insSort(xs[1:]))
10 def ins(x,xs) :
    if xs == [] :
      return [x]
12
    elif x \le xs[0]:
13
      return [x] + xs
14
    else:
15
      return [xs[0]] + ins(x,xs[1:])
16
```

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Python Rewritten

In the style of the abstract algorithm

```
20 def insSortO1(xs):
    if len(xs) <= 1 :
      return xs
22
    else:
23
      (xs1,xs2) = insertionSplit(xs)
24
      vs1 = insSort01(xs1)
25
      vs2 = insSort01(xs2)
26
      ys = insertionJoin(ys1,ys2)
27
28
      return vs
30 def insertionSplit(xs) :
    (xs1.xs2) = (xs[0:1].xs[1:])
    return (xs1,xs2)
32
34def insertionJoin(ys1,ys2) :
    if ys2 == [] :
35
36
      return vs1
37
    elif ys1[0] <= ys2[0] :</pre>
      return ys1 + ys2
38
    else:
39
      return ys2[0:1] + insertionJoin(ys1,ys2[1:])
40
```

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Activity 2 Trace an Evaluation

Insertion Sort — Python Recursive

- Evaluation of insSort([3,0,1,8,7])
- ► Answer goes here

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Activity 2 Trace an Evaluation

Insertion Sort — Python Recursive

► Evaluation of insSort([3,0,1,8,7])

| | Expression to Evaluate | Reason |
|----------|---|----------------|
| | insSort([3,0,1,8,7]) | Initial line 4 |
| - | ins(3, insSort([0,1,8,7])) | line 7 |
| - | ins(3, ins(0, insSort([1,8,7]))) | line 7 |
| - | ins(3, ins(0, ins(1, insSort([8,7])))) | line 7 |
| - | <pre>ins(3, ins(0, ins(1, ins(8, insSort([7])))))</pre> | line 7 |
| - | ins(3, ins(0, ins(1, ins(8, [7])))) | line 5 |
| - | ins(3, ins(0, ins(1, ([7] + ins(8, []))))) | line 15 |
| - | ins(3, ins(0, ins(1, ([7] + [8])))) | line 11 |
| - | ins(3, ins(0, ins(1, [7,8]))) | (+) operator |
| - | ins(3, ins(0, ([1] + [7,8]))) | line 13 |
| - | ins(3, ins(0, [1,7,8])) | (+) operator |
| - | ins(3, ([0] + [1,7,8])) | line 13 |
| - | ins(3, [0,1,7,8]) | (+) operator |
| - | [0] + (ins 3 [1,7,8]) | line 15 |
| - | [0] + ([1] + (ins 3 [7,8])) | line 15 |
| - | [0] + ([1] + ([3] + ([7,8]))) | line 13 |
| → | [0,1,3,7,8] | (+) operator |

- Note that the evaluation consumes more space in the process of evaluation;
- also note that you need to be careful with the brackets when doing an evaluation like this by hand.

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Future Work

The non-recursive version of Insertion sort takes each element in turn and inserts it in the ordered list of elements before it.

```
for index = 1 to (len(xs)-1) do
  insert xs[index] in order in xs[0..index-1]
```

Here is a Python implementation of the above (based on Miller and Ranum (2011, page 215)).

```
42 def insertionSort(xs):
    for index in range(1, len(xs)) :
      currentValue = xs[index]
44
      position = index
45
      while (position > 0) and xs[position - 1] > currentValue :
46
        xs[position] = xs[position - 1]
47
        position = position - 1
48
      xs[position] = currentValue
50
```

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Activity 3

Trace an Evaluation — Python Non-recursive

- Evaluation of insertionSort([3,0,1,8,7])
- Showing just the outer for index loop



► Answer goes here

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Activity 3

Trace an Evaluation — Python Non-recursive

- Evaluation of insertionSort([3,0,1,8,7])
- Showing just the outer for index loop

3 0 1 8 7 start array

3 0 1 8 7 index = 1

0 3 1 8 7 index = 2

0 1 3 8 7 | index = 3

_

0 1 3 8 7 index = 4

0 1 3 7 8 end

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Future Work

Abstract Algorithm

- Selection Split xs1 is the singleton list of the minimum item; xs2 is the original list with the minimum item taken out
- Selection Join just put the minimum item and the sorted xs2 together as the output list

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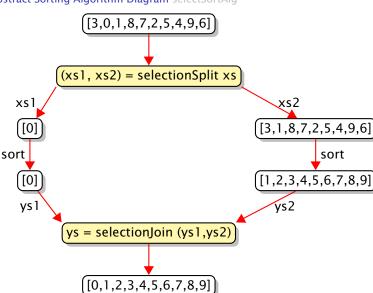
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Python Implementation

```
54 def selSort(xs) :
55   if len(xs) <= 1 :
56    return xs
57   else :
58    minElmnt = min(xs)
59   minIndex = xs.index(minElmnt)
60   xsWithoutMin = xs[:minIndex] + xs[minIndex+1:]
61   return [minElmnt] + selSort(xsWithoutMin)</pre>
```

► Why do we not use xs.remove(min(xs))?

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Future Work

Python Implementation — Question

- ► Why do we not use xs.remove(min(xs))?
- remove() has the side effect of changing the original argument
- ► If we want selSort() to be a function, with no side effects then we should use something else

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Non-recursive Implementation

▶ The non-recursive version of *Selection* sort takes each position of the list in turn and swaps the element at that position with the minimum element in the rest of the list from that position to the end of the list.

```
for fillSlot = 0 to (len(xs) - 2) do
  find the minimum of
    xs[fillSlot+1]..xs[len(xs) - 1]
  and swap with xs[fillSlot]
```

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- ► Here is a Python implementation of the above (based on Miller and Ranum (2011, page 211) but selecting the smallest first not largest, influenced by http://rosettacode.org/wiki/Sorting_algorithms/Selection_sort#PureBasic).
- Note that here we indent by 2 spaces and use the Python idiomatic simultaneous assignment to do the swap in line 71

```
63 def selectionSort(xs) :
    for fillSlot in range(0,len(xs)-1) :
65         minIndex = fillSlot
66    for index in range(fillSlot+1,len(xs)) :
67         if xs[index] < xs[minIndex] :
68             minIndex = index
70    # if fillSlot != minIndex: # only swap if different
71    xs[fillSlot],xs[minIndex] = xs[minIndex],xs[fillSlot]</pre>
```

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Non-recursive Implementation

▶ The non-recursive version of *Selection* sort in Miller & Ranum sorts in ascending order but takes each position of the list in turn from the right end and swaps the element at that position with the maximum element in the rest of the list from the beginning of the list to that position. (Miller and Ranum (2011, page 211))

```
for fillSlot = len(xs) - 1 down to 1 do
  find the maximum of
    xs[0] .. xs[fillSlot]
  and swap with xs[fillSlot]
```

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Here is a Python implementation of the above (based on Miller and Ranum (2011, page 211) selecting the largest first.

```
73 def selSortAscBvMax(xs) :
    for fillSlot in range(len(xs) - 1, 0, -1):
      maxIndex = 0
75
      for index in range(1, fillSlot + 1) :
76
        if xs[index] > xs[maxIndex] :
77
          maxIndex = index
78
      temp = xs[fillSlot]
80
      xs[fillSlot] = xs[maxIndex]
81
      xs[maxIndex] = temp
82
```

Note that both Python non-recursive versions work by side-effect on the input list — they do not return new lists.

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Activity 5

Finding the Non-Recursive Algorithm

For Insertion Sort and Selection Sort discuss how the non-recursive case can be found by considering the recursive case and doing the algorithm in place. Sorting

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- Merge Split xs1 is half the list; xs2 is the other half of the list.
- Merge Join Merge the sorted xs1 and the sorted xs2 together as the output list

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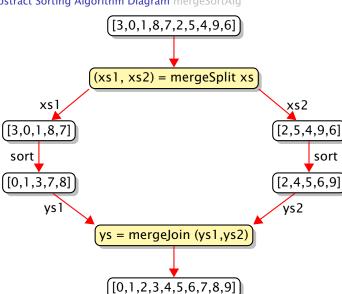
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Python Implementation

```
86 def mergeSort(xs) :
     if len(xs) <= 1 :
      return xs
    else:
89
       (aList,bList) = mergeSplit(xs)
90
      return mergeJoin(mergeSort(aList).mergeSort(bList))
91
93 def mergeSplit(xs):
    return mergeSplit2(xs)
96 def mergeSplit2(xs) :
    half = len(xs)//2
    return (xs[:half],xs[half:])
100 def mergeJoin(xs.vs) :
101
    if xs == [] :
      return ys
102
    elif vs == [] :
103
      return xs
104
    elif xs[0] <= vs[0] :
105
      return [xs[0]] + mergeJoin(xs[1:],ys)
106
    else:
107
      return [ys[0]] + mergeJoin(xs,ys[1:])
108
```

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Python mergeSplit1

```
110 def mergeSplit1(xs) :
111   if len(xs) == 0 :
112    return ([],[])
113   elif len(xs) == 1 :
114   return (xs,[])
115   else :
116   (aList,bList) = mergeSplit1(xs[2:])
117   return ([xs[0]] + aList, [xs[1]] + bList)
```

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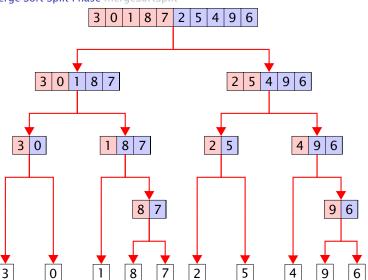
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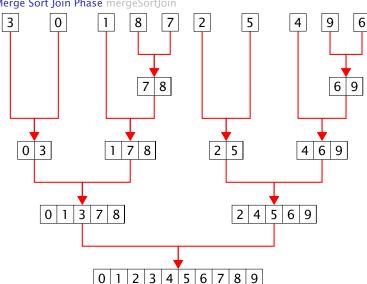
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Future Work

- Here is a Python implementation of the above
- From Miller and Ranum (2011, page 218-221)
- This is also recursive but works in place by changing the array.
- Code from http://interactivepython.org/courselib/ static/pythonds/SortSearch/TheMergeSort.html

```
119 def mergeSortInPlace(xs) :
     if len(xs) > 1:
120
       print("Splitting_", xs)
121
    else:
122
123
       print("Singleton ". xs)
     if len(xs) > 1:
125
       half = len(xs)//2
126
       (aList, bList) = (xs[:half],xs[half:])
127
       mergeSortInPlace(aList)
129
       mergeSortInPlace(bList)
130
```

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References

```
Python In-Place (2)
```

i = i + 1

k = k + 1

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150

```
i.i.k = 0.0.0
132
       while i < len(aList) and j < len(bList) :</pre>
133
          if aList[i] < bList[i] :</pre>
134
            xs[k] = aList[i]
135
            i = i + 1
136
          else:
137
            xs[k] = bList[j]
138
139
            i = i + 1
          k = k + 1
140
       while i < len(aList) :</pre>
142
          xs[k] = aList[i]
143
          i = i + 1
144
          k = k + 1
145
147
       while j < len(bList) :</pre>
          xs[k] = bList[j]
148
```

Python In-Place (3)

▶ Here is the code that reports the merging of the lists

```
if len(xs) > 1:
    print("Merging_", aList, ",", bList, "to", xs)
else :
    print("Merged_", xs)
```

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Python Code Description

- is how the listings package shows spaces in strings by default (read the manual)
- // is the Python integer division operator
- ▶ aList[start:stop:step] is a *slice* of a list see Python Sequence Types — slice operations return a new list (van Rossum and Drake, 2011a, page 19) so xs[:] returns a copy (or clone) of xs — if any of the indices are missing or negative than you have to think a bit (or read the manual)
- In Python you really do need to be aware when you are working with values or references to objects.

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Python In-Place (3)

► A listing of the output of mergeSortInPlace(xsc) below is given in the article version of these notes

```
>>> from SortingPython import *
>>> xs = [3,0,1,8,7,2,5,4,9,6]
>>> xsc = xs[:]
>>> mergeSortInPlace(xsc)
Splitting [3, 0, 1, 8, 7, 2, 5, 4, 9, 6]
#
# lines removed
#
Merging [0, 1, 3, 7, 8] , [2, 4, 5, 6, 9]
to [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
```

No. 11. N.A. - Iv. ...

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Quicksort

Abstract Algorithm

- Quicksort Split Choose an item in the list to be the pivot item; xs1 comprises items in the list less than the pivot plus the pivot; xs2 comprises items in the list greater than or equal to the pivot.
- Quicksort Join just append the sorted xs1 and the sorted xs2 together as the output list

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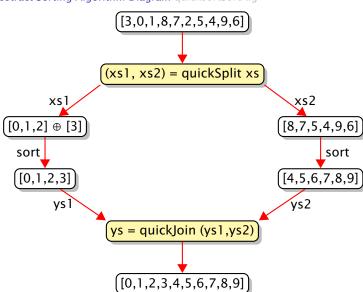
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In Haskell and Python

- Haskell 2010 Language Report section 3.11 List Comprehensions
- $[e \mid q_1, \dots, q_n], n \ge 1$ where q_i qualifiers are either
 - \triangleright generators of the form $p \leftarrow e$ where p is a pattern of type t and e is an expression of type [t]
 - local bindings that provide new definitions for use in the generated expression e or subsequent boolean guards and generators
 - boolean guards which are expressions of type Bool
- Python Language Reference section 6.2.4 Displays for lists, sets and dictionaries and section 6.2.5 List displays
- [expr for target in list] simple comprehension
- [expr for target in list if condition] filters
- [expr for target1 in list1 for target2 in list2] — multiple generators

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► The if test at line 160 shows that Python is weakly typed (and the author of this code comes from JavaScript)

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Quicksort

Python In-Place (1)

- ► The in-place version of Quick sort works by partitioning a list in place about a value pivotvalue: (Azmoodeh, 1990, page 259–266)
- (1) Scan from the left until
 - ► alist[leftmark] >= pivotvalue
- (2) Scan from the right until
 - ► alist[rightmark] < pivotvalue
- (3) Swap alist[leftmark] and alist[rightmark]
- (4) Repeat (1) to (3) until scans meet

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Future Work

- Here is an in place version of Quick Sort from Miller and Ranum (2011, pages 221-226)
- Code based on http://interactivepython.org/courselib/ static/pythonds/SortSearch/TheQuickSort.html

```
168 def quickSort(xs) :
    quickSortHelper(xs, 0, len(xs) - 1)
171 def quickSortHelper(xs, fst, lst) :
172 if fst < lst :
      splitPoint = partition(xs,fst,lst)
174
      quickSortHelper(xs. fst. splitPoint - 1)
176
      quickSortHelper(xs, splitPoint + 1, lst)
177
```

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> Algorithm List Comprehensions Quicksort - Python Quicksort Python

In-Place Rubble Sort

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Future Work

Python In-Place (3)

```
179 def partition(xs.fst.lst):
    pivotValue = xs[fst]
180
    leftMk
                 = fst + 1
181
    riahtMk
              = lst
182
    done
                = False
183
    while not done :
185
186
       while leftMk <= rightMk and \</pre>
                xs[leftMkl <= pivotValue :
187
         leftMk = leftMk + 1
188
       while xs[rightMk] >= pivotValue and \
189
                rightMk >= leftMk :
190
         rightMk = rightMk - 1
191
193
       if rightMk < leftMk :</pre>
194
         done = True
       else:
195
         xs[leftMk], xs[rightMk] = xs[rightMk], xs[leftMk]
196
    xs[fst], xs[rightMk] = xs[rightMk], xs[fst]
198
    return rightMk
199
```

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Quicksort

Python In-Place (4)

- The (\) is enabling a statement to span multiple lines
 see Lutz (2009, page 317), Lutz (2013, page 378)
- for a language that uses the offside rule why do we need to do this?
- Note that using (\) to create continuations is frowned on Lutz (2009, page 318), Lutz (2013, page 379)
- the authors should have put the entire boolean expression inside parentheses () so that we get implicit continuation.
- This is not mentioned explicitly in the Style Guide for Python Code http://www.python.org/dev/peps/pep-0008/ but it does explicitly mention using Python's implicit line joining with layout guidelines.

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In-Place Bubble Sort

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Bubble Sort

Abstract Algorithm

- Bubble sort is rather like the Hello World program of sorting algorithms — we have to include it even it isn't very useful in practice.
- It can be thought of as an in-place version of Selection sort
- ► In the implementations below, in each pass through the list, the next highest item is moved (bubbled) to its proper place.
- OK, I should have written it to bubble the smallest the other way to be consistent with the implementations of Selection sort above.

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Rubble Sort

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Python

- ► Here is a Python implementation from Miller and Ranum (2011, pages 207-210)
- ▶ it does not test if there have been no swaps but does use some knowledge of the algorithm by reducing the pass length by one each time (which the Haskell one did not do)

- Note that range() is a built-in function to Python that is used a lot
- Read the documentation at Section 4.6.6 Ranges
- Remember that range(5) means [0,1,2,3,4] (not [0,1,2,3,4,5] or [1,2,3,4,5])

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Bubble Sort — Abstract Algorithm

Bubble Sort — Python

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- Sorting without comparing items involves calculating a distribution of items to destinations in the correct order.
- The calculation depends on some structure of an item — for example:
 - digits in a numeral
 - letters in a word
- Sorting criteria
- ▶ **Speed** Not ony O(f(n)) or $\Theta(f(n))$ but also the multiplier may be more important $2n^2$ may be faster than $1000n\log n$ for some n
- Smooth or Adaptive the more ordered the input the faster the algorithm
- Stable maintain the relative order of records with equal keys
- Space behaviour should be compact

- Wikipedia: Sorting algorithms with links to Pigeonhole sort, Bucket srt, Radix sort
- Knuth (1998, sec 5.2.5) The Art of Computer Programming Vol. 3: Sorting and Searching Sec 5.2.5 Sorting by Distribution
- Cormen et al (2022, chp 8) Introduction to Algorithms
 Chp 8 Sorting in Linear Time
- Sedgewick and Wayne (2011, sec 5.1) Algorithms Sec 5.1 String Sorts
- Stubbs and Webre (1989, sec 6.4) Data Structures with Abstract Data Types and PASCAL Sec 6.4 Radix Sort
- Rosetta Code: Sorting algorithms/Radix sort rosettacode.org/wiki/Sorting_algorithms/Radix_sort
- Erickson (1989) Algorithms

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- ► Texts from the 1980s similar style to many of texts today
- Aho, Hopcroft, Ullman (1974, sec 3.2) The Design and Analysis of Computer Algorithms sec 3.2 Radix sorting
- Aho, Hopcroft, Ullman (1983, sec 8.5) Data Structures and Algorithms sec 8.5 Bin Sorting
- ► Manber (1989, sec 6.4.1 Bucket Sort and Radix Sort)

 Introduction to Algorithms: A Creative Approach
- ► Reingold and Hansen (1986, sec 8.1.4) *Data Structures* in *Pascal* sec 8.5 Bin Sorting
- ► Tilford and Reingold (1986) Solutions manual to accompany Edward M. Reingold and Wilfred J. Hansen's Data structures in Pascal
- Baase (1988, sec 2.7) Computer Algorithms: Introduction to Design and Analysis sec 2.7 Radix Sorting
- Horowitz and Sahni (1984, sec 7.7) Fundamentals of Data Structures in Pascal sec 7.7 Sorting on Several Keys

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- Edsger W Dijkstra 2001 Note on Teaching Programming
 - It is not only the violin that shapes the violinist, we are all shaped by the the tools we train ourselves to use, and in this respect programming languages have a devious influence: they shape our thinking habits.
- The impact of your choice of programming language will be unknown until you encounter a significantly different language

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- Early procedural programming languages (C, Pascal, Java, Python) tended to offer arrays as their main data structure or the first to be introduced.
- ► Early functional programming languages (Liso, SASL) tended to offer lists as the main or first data structure
- Late, procedural languages adopted lists, associative arrays (dictionaries, maps), sets, type annotations, type systems, generics
- Later, functional languages adopted algebraic data types, advanced type systems
- Both evolved libraries and packaging systems

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Python Development (a)

- The next two sections develop Radix Sort in Python and Haskell to illustrate different approaches
- They are now meant to be model solutions but try to illustrate the influence of each language
- They both follow Bird and Gibbons (2020) Algorithm Design with Haskell Chp 5 Sorting, section 5.4 Bucketsort and Radixsort

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- The fields of the items enable the items to be ordered lexicographically
 - digits for numerals
 - letters for words
 - value and suite for playing cards
- It avoids comparison by creating and distributing elements into buckets according to their radix
 - The base for numerals
 - The range in the alphabet for letters in a word
 - Thirteen buckets for values and 4 for suites in playing cards
- The bucketing process is repeated for each field while preserving the order of the prior step
- Sorting from the least significant field provides a stable sort

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References

Python Development (c)

Some utility functions

```
def concat(xss : list[list]) -> [list] :
    """Takes a list of lists and concatenates them together
    """
    ys = [x for xs in xss for x in xs]
    return ys

def pad(k,xs) :
    """ Pad a list with '0' to length k
    """
    cs = str(xs)
    return replicate(k - len(cs),'0') + cs
```

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Python Development (d)

```
def replicate(n,c) :
    """"" Returns n copies of the character c

    """"

def rep(n,c,base) :
    if n == 0 :
        return base
    else :
        return rep(n-1,c,c + base)

return rep(n,c,'')

def getDigit(n, num) :
    return (str(num)[n])
```

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Python Development (e)

Two functions to partition list of values into a dictionary of buckets

```
def listToKevValues(xs. k) :
      Partitions a list into buckets
  11 11 11
  def lenShow(n) :
    return len(str(n))
  def getDigitPadMaxLen(x) :
    return getDigit(k, pad(maxLen.x))
  \maxLen = \max(\max(lenShow, xs))
  listOfKeyValues = (zip(map(getDigitPadMaxLen,xs),xs))
  return listOfKeyValues
def keyValuesToDict(listKV) :
  kvDict = {str(d): [] for d in range(0,10)}
  for (k,v) in listKV:
    kvDict[k] = kvDict[k] + [v]
  return kyDict
```

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Python Development (f)

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Python Development (g)

```
Pvthon3>>> srtTestData01
[362, 745, 895, 957, 54, 786, 80, 543, 12, 565]
Pvthon3>>> listToDictTest01
{'0': [80], '1': [], '2': [362, 12], '3': [543], '4': [54],
 '5': [745, 895, 565], '6': [786], '7': [957], '8': [], '9': []}
Pvthon3>>> srtTestData02
[80, 362, 12, 543, 54, 745, 895, 565, 786, 957]
Pvthon3>>> listToDictTest02
{'0': [], '1': [12], '2': [], '3': [], '4': [543, 745],
 '5': [54, 957], '6': [362, 565], '7': [],
 '8': [80, 786], '9': [895]}
Pvthon3>>> srtTestData03
[12, 543, 745, 54, 957, 362, 565, 80, 786, 895]
Pvthon3>>> listToDictTest03
{'0': [12, 54, 80], '1': [], '2': [], '3': [362], '4': [],
 '5': [543, 565], '6': [], '7': [745, 786],
 '8': [895]. '9': [957]}
Pvthon3>>> srtTestData04
[12, 54, 80, 362, 543, 565, 745, 786, 895, 957]
```

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Python Development (g)

```
def partitionToList(xs.k) :
  listToDictTest0k = keyValuesToDict(listToKeyValues(xs, k))
  srtTestData0k = concat(list(listToDictTest0k.values()))
  return srtTestDataOk
def radixsort(xs) :
  def lenShow(n) :
    return len(str(n))
  \maxLen = \max(\max(1enShow, xs))
  srtTestData = xs
  for k in range(maxLen - 1, -1, -1):
    srtTestData = partitionToList(srtTestData,k)
  return srtTestData
```

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- This section follows Bird and Gibbons (2020, chp 5) Algorithm Design with Haskell Chp 5 Sorting
- In the chapter both the comparison and npn-comparison sorting algorithms are developed around the view of sorting as a two stage process: first build some kind of tree and then flatten it

```
sortD xs = (flatten . mktree) xs
```

- Function application in Haskell is denoted by juxtaposition — so f x not f(x)
- ightharpoonup The (.) is the function composition operator (f. q) x means f(qx)
- Function application is more binding than (almost) anything else and is left associative — so f x y means (f x) v
- The name sortD is used so not to conflict with builtin sort

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Euture Work

Development

- Items can contain fields which can be used to order the items
- For example, words contain letters
 Integers contain digits
- ► The fields can be extracted by a list of functions, called discriminators, each of which extract one possible field.
- Given a list of discriminators, ds, two elements x and y are lexically ordered if the following returns True

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- Initially we divide the words into piles sorted by their first letter
- ► The piles (or *buckets*) are sortedd the same way but on the next letter and so on
- At the end of this process, there will be a number of little buckets, each containing a single word
- The buckets are then combined in the correct order to give the final sorted list
- We represent the buckets as a tree

```
data TreeD a = LeafD a | NodeD [TreeD a]
```

- This is sometimes called a rose tree
- The data structure allows for buckets to have subbuckets

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Building a rose tree

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```
ptn :: (Bounded b, Enum b, Ord b) -> (a -> b) -> [a] -> [[a]] ptn d xs = [filter (\x -> d x == m) xs | m <- rng] where rng = [ minBound . . maxBound ]
```

- ► The notation \x -> ... is a Lambda abstraction see also Lambda Abstractions
- \x -> x * x is a function (with no name) which squares its argument
- (x -> x * x) 2 evaluates to 2 * 2 and then 4
- The notation in Bird and Gibbons (2020) Algorithm Design with Haskell is

```
\lambda.x expr
```

▶ This is the notation closer to the orignal Maths notation

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```
flatten :: TreeD [a] -> [a]
flatten (LeafD xs) = xs
flatten (NodeD ts) = concatMap flatten ts
bsort ds xs = flatten (mktree ds xs)
```

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```
bsort [] xs = xs
bsort (d : ds) xs = concatMap (bsort ds) (ptn d xs)
```

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► Describe concatMap

```
>>> concatMap (take 3) [[1..], [10..], [100..], [1000..]] [1,2,3,10,11,12,100,101,102,1000,1001,1002]
```

```
map (bsort ds) (ptn d xs) = ptn d (bsort ds xs)
```

```
concatMap (bsort ds) (ptn d xs)
{ above stability property }
= concat (ptn d (bsort ds xs))
```

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► Here is the definition of Radixsort

```
rsort :: (Bounded b,Enum b,Ord b) -> [a -> b] -> [a] -> [a]
rsort [] xs = xs
rsort (d : ds) xs = concat (ptn d (rsort ds xs))
```

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```
ptn :: Ix b => (b,b) -> (a -> b) -> [a] -> [[a]]
ptn (1,u) d xs = elems xa
  where xa = accumArray snoc [] (1, u) (zip (map d xs) xs)
  snoc xs x = xs ++ [x]
```

```
ptn (1, u) d xs = map reverse (elems xa)
  where xa = accumArray (flip (:)) [] (1, u) (zip (map d xs) xs)
```

```
rsort :: Ix b => (b,b) -> [a -> b] -> [a] -> [a]
rsort bb [] xs = xs
rsort bb (d : ds) xs = concat (ptn bb d (rsort bb ds xs))
```

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Discriminator functions

```
discs :: [Int] -> [Int -> Char]
discs xs = [\x -> pad k (show x)!!i | i <- [0..k-1]]
   where k = maximum (map (length . show) xs)
pad k xs = replicate (k - length xs) '0' ++ xs</pre>
```

```
irsort :: [Int] -> [Int]
irsort xs = rsort ('0', '9') (discs xs) xs
```

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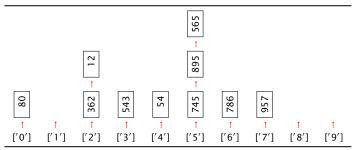
Non-Comparison Sort

Radox Sort

- Radix sort example sort the following list of integers
- Source Stubbs and Webre (1989, sec 6.4.1) Data Structures with Abstract Data Types and PASCAL sec 6.4.1 Example of a Radix Sort

[362, 745, 895, 957, 054, 786, 080, 543, 012, 565]

Stage 1 allocate to buckets on the least significant digit



► This results in

[080,362,012,543,054,745,885,565,786,957]

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Radox Sort Example

 Stage 2 allocate to buckets on the second least significant digit

[080,362,012,543,054,745,885,565,786,957]

| | | | | 745 | 957 | 265 | | 786 | |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| | | | | 1 | 1 | 1 | | 1 | |
| | 012 | | | 543 | 054 | 9 | | 080 | 895 |
| | | | | | | | | | |
| Ī | Ţ | Ţ | Ţ | Ī | Ţ | Ţ | Ţ | 1 | Ţ |
| [0] | [1] | [2] | [3] | [4] | [5] | [6] | [7] | [8] | [9] |

This results in

[012, 543, 745, 054, 957, 362, 565, 080, 885, 786]

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Stage 3 allocate to buckets on the third least significant digit

[012, 543, 745, 054, 957, 362, 565, 080, 786, 895]

| 680 | | | | | | | | | |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| Ţ | | | | | | | | | |
| 054 | | | | | 65 | | 786 | | |
| 0 | | | | | 2 | | _ | | |
| 1 | | | | | 1 | | 1 | | |
| 012 | | | 25 | | 543 | | 745 | 2 | 7 |
| 0 | | | 362 | | 25 | | 7 | 895 | 95 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| [0] | [1] | [2] | [3] | [4] | [5] | [6] | [7] | [8] | [9] |

This results in

[012, 054, 080, 362, 543, 565, 745, 786, 895, 957]

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Radox Sort Example

- ▶ Radix sort further example
- Sorting a pack of cards
- Take a shuffled pack of cards
- ▶ Deal the cards to 13 piles for Ace, 2 through 10, Jack, Queen, King
- Pick up the piles in order
- Deal to 4 piles for Clubs, Diamonds, Hearts, Spades
- Pick up the piles in order
- ► The pack will now be in order

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What Next?

Programming, Debugging, Psychology

Although programming techniques have improved immensely since the early days, the process of finding and correcting errors in programming — known graphically if inelegantly as debugging — still remains a most difficult, confused and unsatisfactory operation. The chief impact of this state of affairs is psychological. Although we are happy to pay lip-service to the adage that to err is human, most of us like to make a small private reservation about our own performance on special occasions when we really try. It is somewhat deflating to be shown publicly and incontrovertibly by a machine that even when we do try, we in fact make just as many mistakes as other people. If your pride cannot recover from this blow, you will never make a programmer.

Christopher Strachey, Scientific American 1966 vol 215 (3) September pp112-124

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What Next?

To err is human?

- To err is human, to really foul things up requires a computer.
- Attributed to Paul R. Ehrlich in 101 Great Programming Quotes
- Attributed to Bill Vaughn in Quote Investigator
- Derived from Alexander Pope (1711, An Essay on Criticism)
- To Err is Humane; to Forgive, Divine
- ► This also contains

A little learning is a dangerous thing; Drink deep, or taste not the Pierian Spring

In programming, this means you have to read the fabulous manual (RTFM)

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Sorting: Motivation

Sorting Taxonomy

Recursion/Iteration
Split/Join Sorting

Non-Comparison Sorts

Future Work

Future Work

Sorting, Searching — very brief summary

- Recursive function definitions
- Inductive data type definitions
 - A list is either an empty list or a first item followed by the rest of the list
 - A binary tree is either an empty tree or a node with an item and two sub-trees
- Recursive definitions often easier to find than iterative
- Sorting
- Searching
- Both use binary tree structure either implicitly or explicitly

Sorting

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Dates

- Sunday 4 January 2026 Tutorial Online Sorting, Recursion
- Sunday 11 January 2026 Tutorial Online Binary Trees, Recursion
- Sunday 8 February 2026 (Module wide) Tutorial Online Binary Trees, Recursion
- ► Tuesday, 10 March 2026 TMA02
- Sunday, 8 March 2026 Tutorial (Online): Graphs, Greedy Algorithms
- Sunday, 12 April 2026 Tutorial (Online): (Module wide) Dynamic Programming
- Sunday, 26 April 2026 Tutorial (Online): (Module wide) Computability, Complexity
- Sunday, 3 May 2026 Tutorial (Online): Review of course material for TMA03
- Tuesday, 26 May 2025 TMA03

Sorting

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Sorting Web Links

- Rosetta Code Sorting Algorithms http: //rosettacode.org/wiki/Sorting_algorithms sorting algorithms implemented n lots of programming languages
- Sorting Algorithm Animations https://www.toptal. com/developers/sorting-algorithms — visual display of the performance of various sorting algorithms for several classes of data: random, nearly sorted, reversed, few unique — worth browsing to.
- Sorting Algorithms as Dances https://www.youtube.com/user/AlgoRythmics inspired!

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References

Sorting Web Links Python Web Links & References

Haskell Web Links & References

Python

Web Links & References

- Miller and Ranum (2011) http://interactivepython.org/courselib/ static/pythonds/index.html — the entire book online with a nice way of running the code.
- ▶ Lutz (2013) one of the best introductory books
- Lutz (2011) a more advanced book earlier editions of these books are still relevant — you can also obtain electronic versions from the O'Reilly Web site http://oreilly.com
- Python 3 Documentation https://docs.python.org/3/
- Python Style Guide PEP 8 https://www.python.org/dev/peps/pep-0008/ (Python Enhancement Proposals)

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Sorts **Future Work**

References

Sorting Web Links Python Web Links & References

Haskell Web Links & References

- Haskell Language https://www.haskell.org
- HaskellWiki https://wiki.haskell.org/Haskell
- Learn You a Haskell for Great Good! very readable introduction to Haskell
- ▶ Bird and Wadler (1988); Bird (1998, 2014) one of the best introductions but tough in parts, requires some mathematical maturity — the three books are in effect different editions
- ▶ Bird and Gibbons (2020) Algorithm Design with Haskell — the descriptions of five main principles of algorithm design: divide and conquer, greedy algorithms, thinning, dynamic programming, and exhaustive search, are mainly language neutral
- ► Functors, Applicatives, and Monads in Pictures a very good outline with cartoons
- Haskell Wikibook

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Haskell Web Links & References

Sorting Algorithms

Demonstration 2 Sorting Algorithms as Dances

- Quicksort
- https://www.youtube.com/user/AlgoRythmics
- the hats make the point(!)

Sorting

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