## Sorting

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Agenda Adobe Connect

Sorting: Motivation

Sorting Taxonomy

Recursion/Iteration
Split/Join Sorting

Future Work

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Sorting M269 Tutorial

Phil Molyneux

5 January 2025

Agenda

- Welcome & introductions
- Tutorial topics: Sorting Algorithms, Recursion
- ► Adobe Connect if you or I get cut off, wait till we reconnect (or send you an email)
- Time: about 1.5 hours
- Do ask questions or raise points.
- Source: of slides, notes, programs and playing cards: M269Tutorial20250105SortingPrsntn2024]/

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References

www.pmolyneux.co.uk/OU/M269FolderSync/M269TutorialNotes/M269Tutorial20250105SortingPrsntn2024J/

- Name Phil Molyneux
- Background
  - Undergraduate: Physics and Maths (Sussex)
  - Postgraduate: Physics (Sussex), Operational Research (Brunel), Computer Science (University College, London)
  - Worked in Operational Research, Business IT, Web technologies, Functional Programming
- First programming languages Fortran, BASIC, Pascal
- Favourite Software
  - ► Haskell pure functional programming language
  - ► Text editors TextMate, Sublime Text previously Emacs
  - ▶ Word processing in <a href="#">MTFX</a> all these slides and notes
  - Mac OS X
- Learning style I read the manual before using the software

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**Future Work** References

- ► Name?
- Favourite software/Programming language?
- Favourite text editor or integrated development environment (IDE)
- List of text editors, Comparison of text editors and Comparison of integrated development environments
- Other OU courses?
- Anything else?

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Interface — Host View



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Web Graphics Recordinas

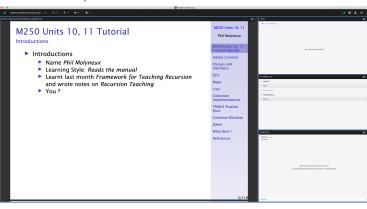
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Interface — Participant View



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## Settings

- Everybody Menu bar Meeting Speaker & Microphone Setup
- Menu bar Microphone Allow Participants to Use Microphone
- Check Participants see the entire slide Workaround
  - Disable Draw Share pod Menu bar Draw icon
  - Fit Width Share pod Bottom bar Fit Width icon
- Meeting Preferences General Host Cursor Show to all attendees
- Menu bar Video Enable Webcam for Participants
- Do not Enable single speaker mode
- Cancel hand tool
- Do not enable green pointer
- Recording Meeting Record Session
- Documents Upload PDF with drag and drop to share pod
- Delete Meeting Manage Meeting Information Uploaded Content and check filename click on delete

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#### Access

Tutor Access

TutorHome M269 Website Tutorials

Cluster Tutorials M269 Online tutorial room

Tutor Groups M269 Online tutor group room

Module-wide Tutorials M269 Online module-wide room

Attendance

TutorHome Students View your tutorial timetables

- Beamer Slide Scaling 440% (422 x 563 mm)
- Clear Everyone's Status

Attendee Pod Menu Clear Everyone's Status

► Grant Access and send link via email

Meeting Manage Access & Entry Invite Participants...

Presenter Only Area

Meeting Enable/Disable Presenter Only Area

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## **Keystroke Shortcuts**

- Keyboard shortcuts in Adobe Connect
- ► Toggle Mic 🛱 + M (Mac), Ctrl + M (Win) (On/Disconnect)
- ► Toggle Raise-Hand status 🗯 + 🖪
- ► Close dialog box (Mac), Esc (Win)
- ► End meeting ∰+\\

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# Adobe Connect Interface

Sharing Screen & Applications

- Share My Screen Application tab Terminal for Terminal
- Share menu Change View Zoom in for mismatch of screen size/resolution (Participants)
- (Presenter) Change to 75% and back to 100% (solves) participants with smaller screen image overlap)
- Leave the application on the original display
- Beware blued hatched rectangles from other (hidden) windows or contextual menus
- Presenter screen pointer affects viewer display beware of moving the pointer away from the application
- First time: System Preferences Security & Privacy Privacy Accessibility

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Adobe Connect Interface

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## **Ending a Meeting**

- Notes for the tutor only
- Tutor:
- ► Recording Meeting Stop Recording ✓
- Remove Participants Meeting End Meeting...
  - Dialog box allows for message with default message:
  - The host has ended this meeting. Thank you for attending.
- Recording availability In course Web site for joining the room, click on the eye icon in the list of recordings under your recording — edit description and name
- Meeting Information Meeting Manage Meeting Information can access a range of information in Web page.
- Delete File Upload Meeting Manage Meeting Information Uploaded Content tab select file(s) and click Delete
- Attendance Report see course Web site for joining room

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#### Invite Attendees

Provide Meeting URL Menu Meeting Manage Access & Entry Invite Participants...

- ► Allow Access without Dialog Menu Meeting

  Manage Meeting Information provides new browser window with Meeting Information Tab bar Edit Information
- ► Check Anyone who has the URL for the meeting can enter the room
- Default Only registered users and accepted guests may enter the room
- Reverts to default next session but URL is fixed
- Guests have blue icon top, registered participants have yellow icon top — same icon if URL is open
- See Start, attend, and manage Adobe Connect meetings and sessions

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Lavouts

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Entering a Room as a Guest (1)

- Click on the link sent in email from the Host
- Get the following on a Web page
- As Guest enter your name and click on Enter Room



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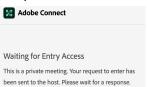
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Entering a Room as a Guest (2)

See the Waiting for Entry Access for Host to give permission



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Entering a Room as a Guest (3)

Host sees the following dialog in Adobe Connect and grants access



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## Layouts

- Creating new layouts example Sharing layout
- Menu Layouts Create New Layout... Create a New Layout dialog

  Create a new blank layout and name it PMolyMain
- New layout has no Pods but does have Layouts Bar open (see Layouts menu)
- Pods
- Menu Pods Share Add New Share and resize/position initial name is Share n— rename PMolyShare
- ► Rename Pod Menu Pods Manage Pods... Manage Pods

  Select Rename Or Double-click & rename
- Add Video pod and resize/reposition
- Add Attendance pod and resize/reposition
- Add Chat pod rename it PMolyChat and resize/reposition

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## Layouts

- Dimensions of Sharing layout (on 27-inch iMac)
  - Width of Video, Attendees, Chat column 14 cm
  - ► Height of Video pod 9 cm
  - ► Height of Attendees pod 12 cm
  - Height of Chat pod 8 cm
- ▶ **Duplicating Layouts** does *not* give new instances of the Pods and is probably not a good idea (apart from local use to avoid delay in reloading Pods)
- Auxiliary Layouts name PMolyAuxOn
  - Create new Share pod
  - Use existing Chat pod
  - Use same Video and Attendance pods

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#### Chat Pods

- Format Chat text
- Chat Pod menu icon My Chat Color
- Choices: Red, Orange, Green, Brown, Purple, Pink, Blue, Black
- Note: Color reverts to Black if you switch layouts
- Chat Pod menu icon Show Timestamps

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# **Graphics Conversion**

PDF to PNG/JPG

- Conversion of the screen snaps for the installation of Anaconda on 1 May 2020
- Using GraphicConverter 11
- File Convert & Modify Conversion Convert
- Select files to convert and destination folder
- ► Click on Start selected Function or 🕱 + 🔎

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# **Adobe Connect Recordings**

## **Exporting Recordings**

- Menu bar Meeting Preferences Video
- Aspect ratio Standard (4:3) (not Wide screen (16:9) default)
- Video quality Full HD (1080p not High default 480p)
- ► Recording Menu bar Meeting Record Session ✓
- Export Recording
- Menu bar Meeting Manage Meeting Information
- New window Recordings check Tutorial Access Type button
- check Public check Allow viewers to download
- Download Recording
- New window Recordings check Tutorial Actions Download File

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## Sorting: Motivation

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# Sorting

### Motivation

- Motivation for studying sorting algorithms
- ► Taxonomy of sorting see Wikipedia Sorting Algorithm
- Abstract comparison sort split/join algorithm
- Insertion sort and selection sort described with split/join algorithm diagram and implemented in Python. (A previous edition also included optional Haskell code)
- Recursive and iterative versions
- Mergesort, Quicksort and Bubble sort in the same framework
- Sorting via a data structure Tree sort
- Comparison sorts and Distribution sorts
- Review of Web sites and sorting algorithms used in practice

- ... virtually every important aspect of programming arises somewhere in the context of sorting or searching.
- How are good algorithms discovered?
- How can given algorithms and programs be improved?
- How can the efficiency of algorithms be analyzed mathematically?
- ► How can a person choose rationally between different algorithms for the same task?
- In what senses can algorithms be proved best possible?
- ► How does the theory of computing interact with practical considerations?

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# **Sorting Algorithms**

Demonstration 1 Sorting Algorithms as Dances

- AlgoRythmics
- Videos tab Insertion Sort
- Insertion Sort
- This is the Romanian folk music that inspired Bartók
- Compare the dance with the Python algorithm for Insertion Sort below

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- Almost everyone has played cards and, as part of any card game, will have sorted cards in their hand
- This exercise is aimed at writing down how you sort you cards and giving these instructions to another person to follow.
- Decide on your general ordering of playing cards you are free to set any ordering you like but here is the usual ordering for suits and values:

```
Clubs < Diamonds < Hearts < Spades
Two < Three < Four < Five < Six
< Seven < Eight < Nine < Ten
< Jack < Oueen < King < Ace
```

▶ Write down your method for sorting cards — the method must specify how to choose a card to move and where to move it to.

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**Future Work** 

Take the 6 cards given below — record the order of the cards



- Using your method, sort the cards record the order of the cards after each move of a card
- Now swap your written method and the cards in your original order with another student.
- Follow the other student's method to sort the cards and record your steps

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# **Activity 1 Card Sorting Exercise**

**Working Space** 

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# Activity 1 Card Sorting Exercise (3)

#### Discussion

- Did both of you end up with the same sequence of steps?
- ▶ Did any of the instructions require human knowledge?
- General point: probably most people use some variation on *Insertion sort* or *Selection sort* but would have steps that had multiple shifts of cards.
- Note: This activity may be done on the Whiteboard using cards from http://pmolyneux.co.uk/OU/M269/ M269TutorialNotes/M269TutorialSorting/Cards/

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# Taxonomy of Sorting Algorithms

## **Comparison Sorts**

- Computational complexity worst, best, average number of comparisons, exchanges and other program contructs (but see http://www.softpanorama.org/ Algorithms/sorting.shtml for Slightly Skeptical View) — O(n²) bad, O(nlog n) better
- Other issues: space behaviour, performance on typical data sets, exchanges versus shifts
- Abstract sorting algorithm Following Merritt (1985, 1997) and Azmoodeh (1990, chp 9), we classify the divide and conquer sorting algorithms by easy/hard split/join
- see diagram below

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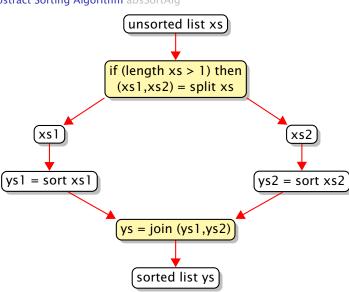
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# Taxonomy of Sorting Algorithms

Abstract Sorting Algorithm absSortAlg



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# Sorting Algorithms

#### Other Classifications

- See Wikipedia Sorting algorithm for big list
- Comparison Sorts
  - Insertion sort, Selection sort, Merge sort, Quicksort, Bubble sort
  - Sorting via a data structure: Tree sort, Heap sort
- Non-Comparison sorts distribution sorts bucket sort, radix sort
- Sorts used in Programming Language Libraries
  - Timsort by Tim Peters used in Python and Java combination of merge and insertion sorts
  - Haskell modified Mergesort by Ian Lynagh in GHC implementation

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- Many functions are naturally defined using recursion
- A recursive function is defined in terms of calls to itself acting on smaller problem instances along with a base case(s) that terminate the recursion
- ► Classic example: Factorial  $n! = n \times (n-1) \cdots 2 \times 1$

```
5def fac(n) :
     return n * fac(n-1)
```

- We can evaluate fac(6) by using a substitution model (section 1.1.5) for function application
- To evaluate a function applied to arguments, evaluate the body of the function with each formal parameter replaced by the corresponding actual arguments. Abelson and Sussman (1996, section 1.1.5) Structure and Interpretation of Computer Programs

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## Evaluation of fac(6)

	Expression to Evaluate	Reason
	fac(6)	Initial line 5
$\rightarrow$	6 * fac(5)	line 8
$\rightarrow$	6 * (5 * fac(4))	line 8
$\rightarrow$	6 * (5 * (4 * fac(3))	line 8
$\rightarrow$	6 * (5 * (4 * (3 * fac(2))))	line 8
$\rightarrow$	6 * (5 * (4 * (3 * (2 * fac(1)))))	line 8
$\rightarrow$	6 * (5 * (4 * (3 * (2 * 1))))	line 6
<b>→</b>	720	Arithmetic

- This occupies more space in the process of evaluation since we cannot do the multiplications until we reach the base case of fac()
- This is a recursive function and a linear recursive process
- Implemented in Python (and most imperative languages) with a stack of function calls
- We can define an equivalent factorial function that produces a different process

### Agenda

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## Split/Join Sorting

**Future Work** 

```
24 def facIter(n) :
25    return accProd(n,1)

27 def accProd(n,x) :
28    if n = 1 :
29        return x
30    else :
31    return accProd(n-1, n * x)
```

- facIter() uses accProd() to maintain a running product and accumulate the final result to return
- We can display the evaluation of facIter(6) using the substitution model

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## Recursion

## Evaluation of facIter(6)

	Expression to Evaluate	Reason
	facIter(6)	Initial line 24
$\rightarrow$	accProd(6,1)	line 25
$\rightarrow$	accProd(5, 6 * 1)	line 30 & (*)
$\rightarrow$	accProd(4, 5 * 6)	line 30 & (*)
$\rightarrow$	accProd(3, 4 * 30)	line 30 & (*)
$\rightarrow$	accProd(2, 3 * 120)	line 30 & (*)
$\rightarrow$	accProd(1, 2 * 360)	line 30 & (*)
$\rightarrow$	720	line 28 & (*)

- This occupies constant space at each stage all the variables describing the state of the calculation are in the function call
- This is a recursive program and an iterative process
- We are assuming the multiplication is evaluated at each function call (strict or eager evaluation)
- Also referred to as tail recursion we need not build a stack of calls

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# Recursion and Iteration

### Iterative Factorial Exercises

- Write a version of the factorial function using a while loop in Python
- Write a version of the factorial function using a for loop in Python

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### Iterative Factorial Exercises — Solutions

Factorial function using a while loop in Python

```
46 def facWhile(n):
47 \quad x = 1
    while n > 1:
49
      x = n * x
50
      n = (n - 1)
51
53
    return x
```

Factorial function using a for loop in Python

```
57 def facFor(n):
x = 1
   for i in range(n,0,-1):
60
     x = i * x
61
63
   return x
```

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## Recursion/Iteration

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**Future Work** References

#### Tail Recursion and Iteration

- ▶ When the structured programming ideas emerged in the 1960s and 1970s the languages such as C and Pascal implemented recursion by always placing the calls on the stack — Python follows this as well
- This means that in those languages they have to have special constructs such as for loops, while loops, to express iterative processes without recursion
- A for loop is syntactically way more complicated than a recursive definition
- Some language implementations (for example, Haskell) spot tail recursion and do not build a stack of calls
- You still have to write your recursion in particular ways to allow the compiler to spot such optimisations.

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- In the late 1980s two books came out that were particularly influential:
- Abelson and Sussman (1984, 1996) Structure and Interpretation of Computer Programs (known as SICP) which was the programming course for the first year at MIT,
- ▶ Bird and Wadler (1988, 1998, 2014) *Introduction to Functional Programming* which was the the programming course for the first year at Oxford.
- See SICP online and Section 1.2 Procedures and the Process They Generate

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References

Structured Programming, GOTO and Recursion (2)

- Dijkstra (1968) Go To Statement Considered Harmful illustrates a debate on structured programming
- ► The von Neumann computer architecture takes the memory and state view of computation as in Turing m/c
- Lambda calculus is equivalent in computational power to a Turing machine (Turing showed this in 1930s) but efficient implementations did not arrive until 1980s
- Functional programming in Lisp or APL was slow
- Alan Perlis (1982) Epigrams on Programming: [Functional programmers] know the value of everything but the cost on nothing
- Erik Meijer (1991) Recursion is the GOTO of functional programming
- Leading to common patterns of higher order functions, map, filter, fold and polymorphic data types

## Split/Join Sorting Algorithms

**Example Algorithms & Implementation** 

- Insertion Sort
- Selection Sort
- Merge Sort
- Quicksort
- Bubble Sort
- Implementations in Python, recursive and non-recursive

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#### Split/Join Sorting

Insertion Sort Selection Sort Merge Sort Quicksort Bubble Sort

Future Work

### **Insertion Sort**

#### **Abstract Algorithm**

- Insertion Split xs1 is the singleton list of the first item; xs2 is the rest of the list
- Insertion Join insert the item in the singleton list into the sorted result of the rest of the list

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Insertion Sort

Insertion Sort — Abstract Algorithm

Insertion Sort — Python Activity 2 — Insertion Sort: Trace an

Evaluation Insertion Sort — Non-recursive

Activity 3 — Insertion Sort Non-recursive Trace

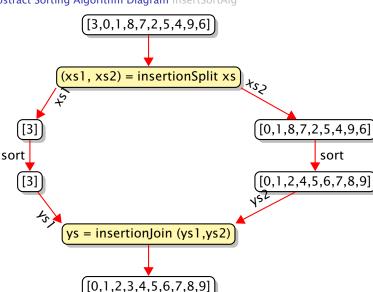
Selection Sort Merge Sort

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### Insertion Sort

Abstract Sorting Algorithm Diagram insertSortAlg



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> Insertion Sort — Abstract Algorithm

Insertion Sort — Python Activity 2 — Insertion Sort: Trace an Evaluation

Insertion Sort —
Non-recursive
Activity 3 — Insertion
Sort Non-recursive

Trace Selection Sort Merge Sort

Merge Sort Quicksort Bubble Sort

Future Work

### Insertion Sort

#### **Python Implementation**

```
4def insSort(xs) :
    if len(xs) \ll 1:
      return xs
    else:
      return ins(xs[0],insSort(xs[1:]))
10 def ins(x,xs) :
    if xs == [] :
      return [x]
12
    elif x \le xs[0]:
13
      return [x] + xs
14
    else:
15
      return [xs[0]] + ins(x,xs[1:])
16
```

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Insertion Sort —
Abstract Algorithm

Insertion Sort — Python

Insertion Sort — Pytho Activity 2 — Insertion Sort: Trace an

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Selection Sort Merge Sort

Quicksort Bubble Sort

Future Work

#### Python Rewritten

In the style of the abstract algorithm

```
20 def insSortO1(xs):
    if len(xs) \ll 1:
      return xs
22
    else:
23
      (xs1,xs2) = insertionSplit(xs)
24
      vs1 = insSort01(xs1)
25
      vs2 = insSort01(xs2)
26
      ys = insertionJoin(ys1,ys2)
27
28
      return vs
30 def insertionSplit(xs) :
    (xs1,xs2) = (xs[0:1],xs[1:])
    return (xs1,xs2)
32
34def insertionJoin(ys1,ys2) :
    if ys2 == [] :
35
36
      return vs1
37
    elif ys1[0] <= ys2[0] :</pre>
      return ys1 + ys2
38
    else:
39
      return ys2[0:1] + insertionJoin(ys1,ys2[1:])
40
```

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## Activity 2 Trace an Evaluation

Insertion Sort — Python Recursive

- Evaluation of insSort([3,0,1,8,7])
- ► Answer goes here

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### Activity 2 Trace an Evaluation

Insertion Sort — Python Recursive

 $\triangleright$  Evaluation of insSort([3,0,1,8,7])

	1= 1 1 1	
	Expression to Evaluate	Reason
	insSort([3,0,1,8,7])	Initial line 4
-	ins(3, insSort([0,1,8,7]))	line 7
-	ins(3, ins(0, insSort([1,8,7])))	line 7
-	ins(3, ins(0, ins(1, insSort([8,7]))))	line 7
-	<pre>ins(3, ins(0, ins(1, ins(8, insSort([7])))))</pre>	line 7
-	ins(3, ins(0, ins(1, ins(8, [7]))))	line 5
-	ins(3, ins(0, ins(1, ([7] + ins(8, [])))))	line 15
-	ins(3, ins(0, ins(1, ([7] + [8]))))	line 11
-	ins(3, ins(0, ins(1, [7,8])))	(+) operator
-	ins(3, ins(0, ([1] + [7,8])))	line 13
-	ins(3, ins(0, [1,7,8]))	(+) operator
-	ins(3, ([0] + [1,7,8]))	line 13
-	ins(3, [0,1,7,8])	(+) operator
-	[0] + (ins 3 [1,7,8])	line 15
-	[0] + ([1] + (ins 3 [7,8]))	line 15
-	[0] + ([1] + ([3] + ([7,8])))	line 13
-	[0,1,3,7,8]	(+) operator

- Note that the evaluation consumes more space in the process of evaluation;
- also note that you need to be careful with the brackets when doing an evaluation like this by hand.

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► The non-recursive version of *Insertion* sort takes each element in turn and inserts it in the ordered list of elements before it.

```
for index = 1 to (len(xs)-1) do
  insert xs[index] in order in xs[0..index-1]
```

Here is a Python implementation of the above (based on Miller and Ranum (2011, page 215)).

```
42 def insertionSort(xs):
43  for index in range(1, len(xs)):
44   currentValue = xs[index]
45   position = index
46   while (position > 0) and xs[position - 1] > currentValue:
47   xs[position] = xs[position - 1]
48   position = position - 1
50   xs[position] = currentValue
```

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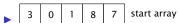
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### **Activity 3**

Trace an Evaluation — Python Non-recursive

- Evaluation of insertionSort([3,0,1,8,7])
- Showing just the outer for index loop



► Answer goes here

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## **Activity 3**

Trace an Evaluation — Python Non-recursive

- Evaluation of insertionSort([3,0,1,8,7])
- Showing just the outer for index loop

3 0 1 8 7 start array

3 0 1 8 7 index = 1

0 3 1 8 7 index = 2

0 1 3 8 7 index = 3

0 1 3 8 7 index = 4

0 1 3 7 8 end

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### **Abstract Algorithm**

- Selection Split xs1 is the singleton list of the minimum item; xs2 is the original list with the minimum item taken out
- Selection Join just put the minimum item and the sorted xs2 together as the output list

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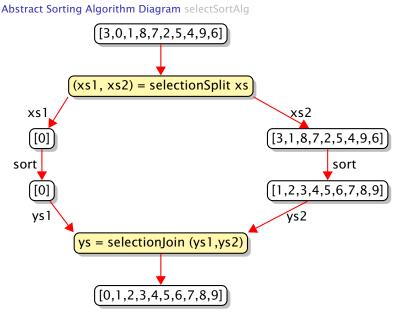
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#### Python Implementation

```
54 def selSort(xs) :
55    if len(xs) <= 1 :
56       return xs
57    else :
58       minElmnt = min(xs)
59       minIndex = xs.index(minElmnt)
60       xsWithoutMin = xs[:minIndex] + xs[minIndex+1:]
61    return [minElmnt] + selSort(xsWithoutMin)</pre>
```

► Why do we not use xs.remove(min(xs))?

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Python Implementation — Question

- ► Why do we not use xs.remove(min(xs))?
- remove() has the side effect of changing the original argument
- ► If we want selSort() to be a function, with no side effects then we should use something else

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#### Non-recursive Implementation

▶ The non-recursive version of *Selection* sort takes each position of the list in turn and swaps the element at that position with the minimum element in the rest of the list from that position to the end of the list.

```
for fillSlot = 0 to (len(xs) - 2) do
  find the minimum of
    xs[fillSlot+1]..xs[len(xs) - 1]
  and swap with xs[fillSlot]
```

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#### Python Non-recursive Implementation

- ► Here is a Python implementation of the above (based on Miller and Ranum (2011, page 211) but selecting the smallest first not largest, influenced by <a href="http://rosettacode.org/wiki/Sorting\_algorithms/Selection\_sort#PureBasic">http://rosettacode.org/wiki/Sorting\_algorithms/Selection\_sort#PureBasic</a>).
- Note that here we indent by 2 spaces and use the Python idiomatic simultaneous assignment to do the swap in line 71

```
63 def selectionSort(xs) :
66     for fillSlot in range(0,len(xs)-1) :
66         minIndex = fillSlot
66     for index in range(fillSlot+1,len(xs)) :
67         if xs[index] < xs[minIndex] :
68             minIndex = index
70     # if fillSlot != minIndex: # only swap if different
71     xs[fillSlot],xs[minIndex] = xs[minIndex],xs[fillSlot]</pre>
```

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#### Selection Sort — Non-recursive

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#### Non-recursive Implementation

▶ The non-recursive version of *Selection* sort in Miller & Ranum sorts in ascending order but takes each position of the list in turn from the right end and swaps the element at that position with the maximum element in the rest of the list from the beginning of the list to that position. (Miller and Ranum (2011, page 211))

```
for fillSlot = len(xs) - 1 down to 1 do
  find the maximum of
    xs[0] .. xs[fillSlot]
  and swap with xs[fillSlot]
```

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#### Python Non-recursive Implementation

Here is a Python implementation of the above (based on Miller and Ranum (2011, page 211) selecting the largest first.

```
73 def selSortAscBvMax(xs) :
    for fillSlot in range(len(xs) - 1, 0, -1):
      maxIndex = 0
75
      for index in range(1, fillSlot + 1) :
76
        if xs[index] > xs[maxIndex] :
77
          maxIndex = index
78
      temp = xs[fillSlot]
80
      xs[fillSlot] = xs[maxIndex]
81
      xs[maxIndex] = temp
82
```

► Note that both Python non-recursive versions work by side-effect on the input list — they do not return new lists.

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### **Activity 5**

#### Finding the Non-Recursive Algorithm

► For *Insertion Sort* and *Selection Sort* discuss how the non-recursive case can be found by considering the recursive case and doing the algorithm in place.

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## Merge Sort

### **Abstract Algorithm**

- Merge Split xs1 is half the list; xs2 is the other half of the list.
- Merge Join Merge the sorted xs1 and the sorted xs2 together as the output list

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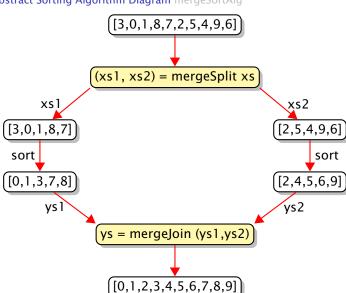
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## Merge Sort

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### Python Implementation

```
86 def mergeSort(xs) :
     if len(xs) <= 1 :
      return xs
    else:
89
       (aList,bList) = mergeSplit(xs)
90
      return mergeJoin(mergeSort(aList).mergeSort(bList))
91
93 def mergeSplit(xs):
    return mergeSplit2(xs)
96 def mergeSplit2(xs) :
    half = len(xs)//2
    return (xs[:half],xs[half:])
100 def mergeJoin(xs.vs) :
101
    if xs == [] :
      return ys
102
    elif vs == [] :
103
      return xs
104
    elif xs[0] <= vs[0] :
105
      return [xs[0]] + mergeJoin(xs[1:],ys)
106
    else:
107
      return [ys[0]] + mergeJoin(xs,ys[1:])
108
```

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**Future Work** 

### Merge Sort

### Python mergeSplit1

```
110 def mergeSplit1(xs) :
111    if len(xs) == 0 :
112      return ([],[])
113    elif len(xs) == 1 :
114      return (xs,[])
115    else :
116      (aList,bList) = mergeSplit1(xs[2:])
117    return ([xs[0]] + aList, [xs[1]] + bList)
```

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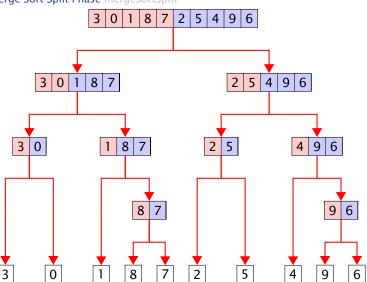
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## Merge Sort Diagram

Merge Sort Split Phase mergeSortSplit



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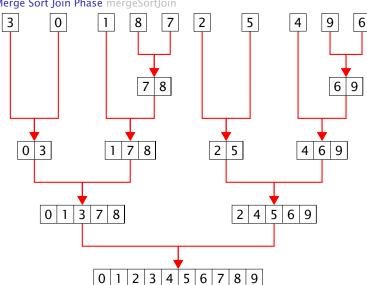
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## Merge Sort Diagram

Merge Sort Join Phase mergeSortJoin



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**Future Work** 

- Python In-Place (1)
  - Here is a Python implementation of the above
  - From Miller and Ranum (2011, page 218-221)
  - This is also recursive but works in place by changing the array.
  - Code from http://interactivepython.org/courselib/ static/pythonds/SortSearch/TheMergeSort.html

```
119 def mergeSortInPlace(xs) :
     if len(xs) > 1:
120
       print("Splitting_", xs)
121
    else:
122
123
       print("Singleton ". xs)
     if len(xs) > 1:
125
       half = len(xs)//2
126
       (aList, bList) = (xs[:half],xs[half:])
127
       mergeSortInPlace(aList)
129
       mergeSortInPlace(bList)
130
```

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### Python In-Place (2)

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```
i,j,k = 0,0,0
132
       while i < len(aList) and j < len(bList) :</pre>
133
          if aList[i] < bList[i] :</pre>
134
            xs[k] = aList[i]
135
            i = i + 1
136
          else:
137
            xs[k] = bList[j]
138
139
            i = i + 1
          k = k + 1
140
       while i < len(aList) :</pre>
142
          xs[k] = aList[i]
143
          i = i + 1
144
          k = k + 1
145
       while j < len(bList) :</pre>
147
          xs[k] = bList[j]
148
          j = j + 1
149
          k = k + 1
```

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### **Future Work**

### Merge Sort

Python In-Place (3)

▶ Here is the code that reports the merging of the lists

```
if len(xs) > 1:
    print("Merging_", aList, ",", bList, "to", xs)
else :
    print("Merged_", xs)
```

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### Merge Sort

### Python Code Description

- is how the listings package shows spaces in strings by default (read the manual)
- // is the Python integer division operator
- ▶ aList[start:stop:step] is a *slice* of a list see Python Sequence Types — slice operations return a new list (van Rossum and Drake, 2011a, page 19) so xs[:] returns a copy (or clone) of xs — if any of the indices are missing or negative than you have to think a bit (or read the manual)
- In Python you really do need to be aware when you are working with values or references to objects.

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#### Python In-Place (3)

A listing of the output of mergeSortInPlace(xsc) below is given in the article version of these notes

```
>>> from SortingPython import *
 >>> xs = [3,0,1,8,7,2,5,4,9,6]
 >>> xsc = xs[:]
 >>> mergeSortInPlace(xsc)
 Splitting [3, 0, 1, 8, 7, 2, 5, 4, 9, 6]
   lines removed
Merging [0, 1, 3, 7, 8], [2, 4, 5, 6, 9] to [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
```

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### Quicksort

#### **Abstract Algorithm**

- Quicksort Split Choose an item in the list to be the pivot item; xs1 comprises items in the list less than the pivot plus the pivot; xs2 comprises items in the list greater than or equal to the pivot.
- Quicksort Join just append the sorted xs1 and the sorted xs2 together as the output list

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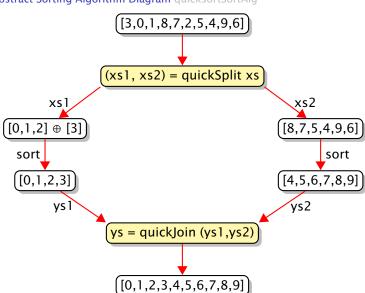
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# List Comprehensions

In Haskell and Python

- Haskell 2010 Language Report section 3.11 List Comprehensions
- $[e \mid q_1, \dots, q_n], n \ge 1$  where  $q_i$  qualifiers are either
  - $\triangleright$  generators of the form  $p \leftarrow e$  where p is a pattern of type t and e is an expression of type [t]
  - local bindings that provide new definitions for use in the generated expression e or subsequent boolean guards and generators
  - boolean guards which are expressions of type Bool
- Python Language Reference section 6.2.4 Displays for lists, sets and dictionaries and section 6.2.5 List displays
- [ expr for target in list] simple comprehension
- [ expr for target in list if condition] filters
- [ expr for target1 in list1 for target2 in list2] — multiple generators

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## Quicksort

#### **Python**

► The if test at line 160 shows that Python is weakly typed (and the author of this code comes from lavaScript)

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### Quicksort

#### Python In-Place (1)

- The in-place version of Quick sort works by partitioning a list in place about a value pivotvalue: (Azmoodeh, 1990, page 259-266)
- (1) Scan from the left until
  - ► alist[leftmark] >= pivotvalue
- (2) Scan from the right until
  - ► alist[rightmark] < pivotvalue
- (3) Swap alist[leftmark] and alist[rightmark]
- (4) Repeat (1) to (3) until scans meet

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- Here is an in place version of Quick Sort from Miller and Ranum (2011, pages 221-226)
- Code based on http://interactivepython.org/courselib/ static/pythonds/SortSearch/TheQuickSort.html

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```
179 def partition(xs.fst.lst):
    pivotValue = xs[fst]
180
    leftMk
                 = fst + 1
181
    riahtMk
              = 1st
182
    done
                = False
183
    while not done :
185
186
       while leftMk <= rightMk and \</pre>
                xs[leftMkl <= pivotValue :
187
         leftMk = leftMk + 1
188
       while xs[rightMk] >= pivotValue and \
189
                rightMk >= leftMk :
190
         rightMk = rightMk - 1
191
193
       if rightMk < leftMk :</pre>
194
         done = True
       else:
195
         xs[leftMk], xs[rightMk] = xs[rightMk], xs[leftMk]
196
    xs[fst], xs[rightMk] = xs[rightMk], xs[fst]
198
    return rightMk
199
```

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### Quicksort

#### Python In-Place (4)

- ▶ The (\) is enabling a statement to span multiple lines see Lutz (2009, page 317), Lutz (2013, page 378)
- for a language that uses the offside rule why do we need to do this?
- Note that using (\) to create continuations is frowned on Lutz (2009, page 318), Lutz (2013, page 379)
- the authors should have put the entire boolean expression inside parentheses () so that we get implicit continuation.
- This is not mentioned explicitly in the Style Guide for Pvthon Code http://www.python.org/dev/peps/pep-0008/ but it does explicitly mention using Python's implicit line joining with layout guidelines.

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**Ouicksort Python** In-Place Rubble Sort

**Euture Work** 

### **Bubble Sort**

#### Abstract Algorithm

- Bubble sort is rather like the Hello World program of sorting algorithms — we have to include it even it isn't very useful in practice.
- It can be thought of as an in-place version of Selection sort
- ► In the implementations below, in each pass through the list, the next highest item is moved (bubbled) to its proper place.
- OK, I should have written it to bubble the smallest the other way to be consistent with the implementations of Selection sort above.

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Bubble Sort — Abstract Algorithm

Bubble Sort — Python

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#### Python

- ► Here is a Python implementation from Miller and Ranum (2011, pages 207–210)
- ▶ it does not test if there have been no swaps but does use some knowledge of the algorithm by reducing the pass length by one each time (which the Haskell one did not do)

- Note that range() is a built-in function to Python that is used a lot
- Read the documentation at Section 4.6.6 Ranges
- Remember that range(5) means [0,1,2,3,4] (not [0,1,2,3,4,5] or [1,2,3,4,5])

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### What Next?

Programming, Debugging, Psychology

Although programming techniques have improved immensely since the early days, the process of finding and correcting errors in programming — known graphically if inelegantly as debugging — still remains a most difficult, confused and unsatisfactory operation. The chief impact of this state of affairs is psychological. Although we are happy to pay lip-service to the adage that to err is human, most of us like to make a small private reservation about our own performance on special occasions when we really try. It is somewhat deflating to be shown publicly and incontrovertibly by a machine that even when we do try, we in fact make just as many mistakes as other people. If your pride cannot recover from this blow, you will never make a programmer.

Christopher Strachey, Scientific American 1966 vol 215 (3) September pp112-124

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#### To err is human?

- To err is human, to really foul things up requires a computer.
- Attributed to Paul R. Ehrlich in 101 Great Programming Quotes
- Attributed to Bill Vaughn in Quote Investigator
- Derived from Alexander Pope (1711, An Essay on Criticism)
- To Err is Humane; to Forgive, Divine
- This also contains

A little learning is a dangerous thing; Drink deep, or taste not the Pierian Spring

In programming, this means you have to read the fabulous manual (RTFM)

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### **Future Work**

Sorting, Searching — very brief summary

- Recursive function definitions
- Inductive data type definitions
  - A *list* is either an empty list or a first item followed by the rest of the list
  - A binary tree is either an empty tree or a node with an item and two sub-trees
- Recursive definitions often easier to find than iterative
- Sorting
- Searching
- Both use binary tree structure either implicitly or explicitly

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- Sunday 5 January 2025 Tutorial Online Sorting, Recursion
- Sunday 12 January 2025 Tutorial Online Binary Trees, Recursion
- Sunday 9 February 2025 (Module wide) Tutorial Online Binary Trees, Recursion
- Thursday, 13 March 2025 TMA02
- Sunday, 9 March 2025 Tutorial (Online): Graphs, Greedy **Algorithms**
- Sunday, 6 April 2025 Tutorial (Online): (Module wide) Dynamic Programming
- Sunday, 27 April 2025 Tutorial (Online): (Module wide) Computability, Complexity
- Sunday, 4 May 2025 Tutorial (Online): Review of course material for TMA03
- Thursday, 8 May 2025 TMA03

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# Sorting

Web Links

- ► Rosetta Code Sorting Algorithms http: //rosettacode.org/wiki/Sorting\_algorithms sorting algorithms implemented n lots of programming languages
- Sorting Algorithm Animations https://www.toptal.com/developers/sorting-algorithms visual display of the performance of various sorting algorithms for several classes of data: random, nearly sorted, reversed, few unique worth browsing to.
- Sorting Algorithms as Dances https://www.youtube.com/user/AlgoRythmics inspired!

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References
Sorting Web Links

Python Web Links & References Haskell Web Links & References

Demonstration 2 Sorting Algorithms as Dances

### **Python**

#### Web Links & References

- Miller and Ranum (2011) http://interactivepython.org/courselib/ static/pythonds/index.html — the entire book online with a nice way of running the code.
- ▶ Lutz (2013) one of the best introductory books
- Lutz (2011) a more advanced book earlier editions of these books are still relevant — you can also obtain electronic versions from the O'Reilly Web site http://oreilly.com
- Python 3 Documentation https://docs.python.org/3/
- Python Style Guide PEP 8 https://www.python.org/dev/peps/pep-0008/ (Python Enhancement Proposals)

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### References

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#### Haskell Web Links & References

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- Haskell Language https://www.haskell.org
- HaskellWiki https://wiki.haskell.org/Haskell
- Learn You a Haskell for Great Good! very readable introduction to Haskell
- ▶ Bird and Wadler (1988); Bird (1998, 2014) one of the best introductions but tough in parts, requires some mathematical maturity — the three books are in effect different editions
- ▶ Bird and Gibbons (2020) Algorithm Design with Haskell — the descriptions of five main principles of algorithm design: divide and conquer, greedy algorithms, thinning, dynamic programming, and exhaustive search, are mainly language neutral
- ► Functors, Applicatives, and Monads in Pictures a very good outline with cartoons
- Haskell Wikibook

## **Sorting Algorithms**

Demonstration 2 Sorting Algorithms as Dances

- Quicksort
- ▶ https://www.youtube.com/user/AlgoRythmics
- the hats make the point(!)

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