# M269 Python, Logic, ADTs M269 Units 1, 2

Phil Molyneux

5 December 2020

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Adobe Connect Programming

Python

Complexity

Logarithms

Before Calculators

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Haskell Example References

# M269 Tutorial: Python, Logic, ADTs

Agenda

- Introductions
- Programming Paradigms and Step-by-Step Guide
- Programming and Python
- Complexity and Big O Notation
- ...with a little classical logic
- Abstract Data Type examples
- A look towards the next Units
  - Recursive function definitions
  - Inductive data type definitions

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Introductions, Admin, Web Sites

Introductions

Name Phil Molyneux

Learning Style Reads the manual

Learnt last month Framework for ADT vs OO and wrote notes on Monads to encapsulate programming with effects

Read Stack Overflow Annual Developer Survey

Read Programming Languages Survey

► You?

Do ask questions or raise points

More material here that we can cover, some reference

pmolyneux.co.uk/OU/M269FolderSync/M269TutorialNotes/M269TutorialProgPythonADT/

Complexity example: M269TutorialProgPythonADT.py

Rail Ticket example: M269TutorialProgPythonADT01.py

Queue ADT example: M269TutorialProgPythonADT02Queue.py

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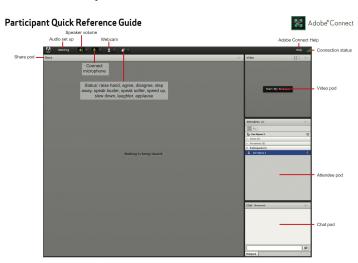
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Interface — Student Quick Reference



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#### Settings

- Everybody: Audio Settings Meeting Audio Setup Wizard...
- ► Audio Menu bar Audio Microphone rights for Participants ✓
- Do not Enable single speaker mode
- ► Drawing Tools Share pod menu bar Draw (1 slide/screen)
- Share pod menu bar Menu icon Enable Participants to draw gray
- Meeting Preferences Whiteboard Enable Participants to draw
- Cancel hand tool
- Do not enable green pointer...
- Meeting Preferences Attendees Pod Disable Raise Hand notification
- Cursor Meeting Preferences General tab Host Cursors
  Show to all attendees ✓ (default Off)
- Meeting Preferences Screen Share Cursor Show Application Cursor
- ► Webcam Menu bar Webcam Enable Webcam for Participants ✓
- ► Recording Meeting Record Meeting... ✓

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#### Access

Tutor Access

TutorHome M269 Website Tutorials

Cluster Tutorials M269 Online tutorial room

Tutor Groups M269 Online tutor group room

Module-wide Tutorials M269 Online module-wide room

Attendance

TutorHome Students View your tutorial timetables

- ► Beamer Slide Scaling 440% (422 x 563 mm)
- Clear Everyone's Status

Attendee Pod Menu Clear Everyone's Status

Grant Access and send link via email

Meeting Manage Access & Entry Invite Participants...

Presenter Only Area

Meeting Enable/Disable Presenter Only Area

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#### **Keystroke Shortcuts**

- Keyboard shortcuts in Adobe Connect
- ► Toggle Mic 🖁 + M (Mac), Ctrl + M (Win) (On/Disconnect)
- ► Close dialog box (Mac), Esc (Win)
- ▶ End meeting ★ \

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### **Adobe Connect Interface**

Student View (default)



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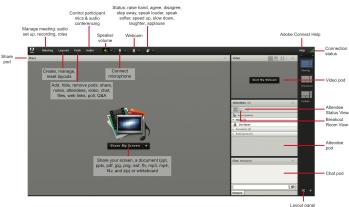
Haskell Example

### Adobe Connect Interface

**Tutor View** 

# Host Quick Reference Guide





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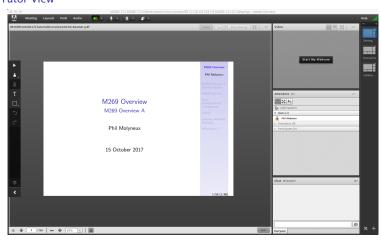
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### **Adobe Connect Interface**

#### **Tutor View**



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- Share My Screen Application tab Terminal for Terminal
- Share menu Change View Zoom in for mismatch of screen size/resolution (Participants)
- (Presenter) Change to 75% and back to 100% (solves participants with smaller screen image overlap)
- Leave the application on the original display
- Beware blued hatched rectangles from other (hidden) windows or contextual menus
- Presenter screen pointer affects viewer display beware of moving the pointer away from the application
- First time: System Preferences Security & Privacy Privacy Accessibility

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#### **Ending a Meeting**

- Notes for the tutor only
- Student: Meeting Exit Adobe Connect
- ► Tutor:
- ► Recording Meeting Stop Recording ✓
- Remove Participants Meeting End Meeting...
  - Dialog box allows for message with default message:
  - The host has ended this meeting. Thank you for attending.
- Recording availability In course Web site for joining the room, click on the eye icon in the list of recordings under your recording — edit description and name
- Meeting Information Meeting Manage Meeting Information can access a range of information in Web page.
- Attendance Report see course Web site for joining room

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Invite Attendees

Provide Meeting URL Menu Meeting Manage Access & Entry Invite Participants...

Allow Access without Dialog Menu Meeting Manage Meeting Information provides new browser window with Meeting Information Tab bar Edit Information

- Check Anyone who has the URL for the meeting can enter the room
- ▶ Default Only registered users and accepted guests may enter the room
- Reverts to default next session but URL is fixed
- Guests have blue icon top, registered participants have yellow icon top — same icon if URL is open
- See Start, attend, and manage Adobe Connect meetings and sessions

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#### Layouts

Creating new layouts example Sharing layout

Menu Layouts Create New Layout... Create a New Layout dialog
Create a new blank layout and name it PMolyMain

- New layout has no Pods but does have Layouts Bar open (see Layouts menu)
- Pods
- Menu Pods Share Add New Share and resize/position initial name is Share n
- Rename Pod Menu Pods Manage Pods... Manage Pods

  Select Rename Or Double-click & rename
- Add Video pod and resize/reposition
- Add Attendance pod and resize/reposition
- Add Chat pod name it PMolyChat and resize/reposition

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#### Layouts

- Dimensions of Sharing layout (on 27-inch iMac)
  - Width of Video, Attendees, Chat column 14 cm
  - Height of Video pod 9 cm
  - Height of Attendees pod 12 cm
  - ► Height of Chat pod 8 cm
- Duplicating Layouts does not give new instances of the Pods and is probably not a good idea (apart from local use to avoid delay in reloading Pods)

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#### Chat Pods

- Format Chat text
- Chat Pod menu icon My Chat Color
- Choices: Red, Orange, Green, Brown, Purple, Pink, Blue, Black
- Note: Color reverts to Black if you switch layouts
- Chat Pod menu icon Show Timestamps

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Imperative or procedural programming has statements which can manipulate global memory, have explicit control flow and can be organised into procedures (or functions)

**Sequence** of statements

```
stmnt ; stmnt
```

Iteration to repeat statements

```
while expr :
   suite

for targetList in exprList :
   suite
```

Selection choosing between statements

```
if expr : suite
elif expr : suite
else : suite
```

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Haskell Example

Functional programming treats computation as the evaluation of expressions and the definition of functions (in the mathematical sense)

► Function composition to combine the application of two or more functions — like sequence but from right to left (notation accident of history)

$$(f . g) x = f (g x)$$

- Recursion function definition defined in terms of calls to itself (with *smaller* arguments) and base case(s) which do not call itself.
- Conditional expressions choosing between alternatives expressions

if expr then expr else expr

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## Computation

Programming, Programming Languages

- M269 is not a programming course but . . .
- The course uses Python to illustrate various algorithms and data structures
- ► The final unit addresses the question:
- What is an algorithm? What is programming? What is a programming language?
- So it is a programming course (sort of)

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#### Searching

- Given an ordered list (xs) and a value (va1), return
  - Position of val in xs or
  - Some indication if val is not present
- Simple strategy: check each value in the list in turn
- Better strategy: use the ordered property of the list to reduce the range of the list to be searched each turn
  - Set a range of the list
  - If val equals the mid point of the list, return the mid point
  - Otherwise half the range to search
  - If the range becomes negative, report not present (return some distinguished value)

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Haskell Example

Binary Search Iterative

```
idef binarySearchIter(xs.val):
   lo = 0
    hi = len(xs) - 1
    while lo <= hi:
      mid = (lo + hi) // 2
6
      quess = xs[mid]
7
      if val == guess:
9
        return mid
10
      elif val < guess:
11
        hi = mid - 1
12
      else:
13
        lo = mid + 1
14
16
    return None
```

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Haskell Example

**Binary Search Recursive** 

```
17 def binarySearchRec(xs.val.lo=0.hi=-1):
    if (hi == -1):
      hi = len(xs) - 1
19
   mid = (lo + hi) // 2
21
    if hi < lo:
23
24
      return None
    else:
25
26
      quess = xs[mid]
      if val == quess:
27
        return mid
28
      elif val < guess:
29
        return binarySearchRec(xs,val,lo,mid-1)
30
      else:
31
32
        return binarySearchRec(xs,val,mid+1,hi)
```

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Binary Search — Exercise

Given the Python definition of binarySearchRec from above, trace an evaluation of binarySearchRec(xs, 25) where xs is

xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95]

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```
Binary Search — Solution
```

```
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs, 25)
```

XS = Highlight the mid value and search range
binarySearchRec(xs,25,??,??)

XS = Highlight the mid value and search range
binarySearchRec(xs,25,??,??)

XS = Highlight the mid value and search range
binarySearchRec(xs,25,??,??)

XS = Highlight the mid value and search range
binarySearchRec(xs,25,??,??)

Return value: ??

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```
Binary Search — Solution
```

```
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs, 25)
```

```
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs,25,??,??)
```

```
XS = Highlight the mid value and search range
binarySearchRec(xs,25,??,??)
```

```
XS = Highlight the mid value and search range
binarySearchRec(xs,25,??,??)
```

```
XS = Highlight the mid value and search range
binarySearchRec(xs,25,??,??)
```

Return value: ??

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Binary Search — Solution

```
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs, 25)
```

xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95] binarySearchRec(xs,25,8,14) by line 31

XS = Highlight the mid value and search range

binarySearchRec(xs,25,??,??)

XS = Highlight the mid value and search range
binarySearchRec(xs,25,??,??)

XS = Highlight the mid value and search range
binarySearchRec(xs,25,??,??)

Return value: ??

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```
Binary Search — Solution
```

Return value: ??

```
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95] binarySearchRec(xs, 25) 
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95] binarySearchRec(xs,25,8,14) by line 31 
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95] binarySearchRec(xs,25,??,??) 
xS = Highlight the mid value and search range binarySearchRec(xs,25,??,??) 
xS = Highlight the mid value and search range binarySearchRec(xs,25,??,??)
```

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```
Binary Search — Solution
```

```
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs, 25)
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs,25,8,14) by line 31
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs,25,8,10) by line 31
xS = Highlight the mid value and search range
binarySearchRec(xs,25,??,??)
xS = Highlight the mid value and search range
binarySearchRec(xs,25,??,??)
Return value: ??
```

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```
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xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs, 25)
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs, 25, 8, 14) by line 31
xs = [2.5,7.15,17.19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs, 25, 8, 10) by line 31
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87.95]
binarySearchRec(xs, 25, ??, ??)
XS = Highlight the mid value and search range
binarySearchRec(xs, 25, ??, ??)
Return value: ??
```

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```
Binary Search — Solution
```

```
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binarySearchRec(xs, 25)
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xs = [2.5,7.15,17.19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs, 25, 8, 10) by line 31
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs, 25, 8, 8) by line 29
XS = Highlight the mid value and search range
binarySearchRec(xs, 25, ??, ??)
Return value: ??
```

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binarySearchRec(xs, 25, 8, 10) by line 31
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binarySearchRec(xs, 25, 8, 8) by line 29
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs,25,??,??)
Return value: ??
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xs = [2.5,7.15,17.19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs, 25, 8, 10) by line 31
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs, 25, 8, 8) by line 29
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs, 25, 8, 7) by line 29
Return value: ??
```

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Binary Search — Solution

```
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs, 25)
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs, 25, 8, 14) by line 31
xs = [2.5,7.15,17.19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs, 25, 8, 10) by line 31
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs, 25, 8, 8) by line 29
xs = [2,5,7,15,17,19,21,24,27,31,37,48,57,87,95]
binarySearchRec(xs, 25, 8, 7) by line 29
Return value: None by line 23
```

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- Both forms compare the given value (val) to the mid-point value of the range of the list (xs[mid])
- If not found, the range is adjusted via assignment in a while loop (iterative) or function call (recursive)
- ► The recursive version has default parameter values to initialise the function call (evil, should be a helper function)
- There are two base cases:
  - The value is found (val == guess)
  - ► The range becomes negative (hi < 1o)
- ▶ The return value is either mid or None
- ▶ What is the *type* of the binary search function?

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Binary Search — Performance

- ► *Linear search* number of comparisons
  - Best case 1 (first item in the list)
  - Worst case n (last item)
  - Average case  $\frac{1}{2}$ n
- ▶ *Binary search* number of comparisons
  - Best case 1 (middle item in the list)
  - ► Worst case log<sub>2</sub> n (steps to see all)
  - Average case  $\log_2 n 1$  (steps to see half)

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f---- C-l---l--

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- 1. Invent a *name* for the program (or function)
- 2. What is the type of the function? What sort of input does it take and what sort of output does it produce? In Python a type is implicit; in other languages such as Haskell a type signature can be explicit.
- 3. Invent *names* for the input(s) to the function (*formal* parameters) — this can involve thinking about possible patterns or data structures
- 4. What restrictions are there on the input state the preconditions.
- 5. What must be true of the output state the postconditions.
- 6. Think of the definition of the function body.

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Haskell Example

- Think of an example or two what should the program/function do?
- 2. Break the inputs into separate cases.
- 3. Deal with simple cases.
- 4. Think about the result try your examples again.

### Thinking Strategies

- 1. Don't think too much at one go break the problem down. Top down design, step-wise refinement.
- 2. What are the inputs describe all the cases.
- 3. Investigate choices. What data structures ? What algorithms ?
- 4. Use common tools bottom up synthesis.
- Spot common function application patterns generalise & then specialise.
- 6. Look for good  ${\it glue}$  to combine functions together.

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### **Python**

Learning Python

- Miller & Ranum Problem Solving with Algorithms and Data Structures using Python
- Python 3 Documentation
- Python Tutorial
- ► Python Language Reference
- ► Python Library Reference
- ► Hitchhiker's Guide to Python
- Stackoverflow on Python
- ▶ Dive into Python 3

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### **Python**

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Install ActivePython version 3.x from http: //www.activestate.com/activepython/downloads

- Mac OS X Python 3 is at /usr/local/bin/python3.3 which is a symbolic link to /Library/Frameworks/ Python.framework/Versions/3.3/bin/python3.3
- Mac OS X idle 3 is at /usr/local/bin/idle3.3 (exact versions will depend on install date)
- Windows install location %SystemDrive%\Python33 and in Start menu (if Windows 7)
- Documentation at http://docs.activestate.com/activepython/3.3/
- Mac OS X may need to install correct version of Tcl/tk for IDLE —

https://www.python.org/download/mac/tcltk

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### **Python**

### Setting up Python with Komodo 2

- ► Install the M269 Komodo macros
  - See M269 Software Installation
  - Make sure the Toolbox and Command output tabs are visible View Tabs & Sidebars
  - Right-Click in *Toolbox* and select Add New Folder... to create M269 folder in *Toolbox*
  - Select M269 folder, right-click and select Import/Export Import Files from File System and select both files from the M269 macro download.
- Ensure Komodo is using Python 3
  - Preferences... Languages Category Python 3 and select your Python 3
  - In the Toolbox right-click Run Python File and select Properties

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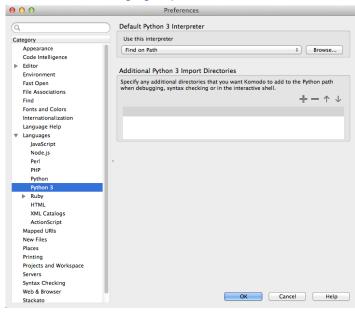
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### Komodo Preferences: Languages Python 3



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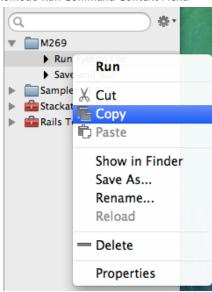
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Komodo Run Command Context Menu



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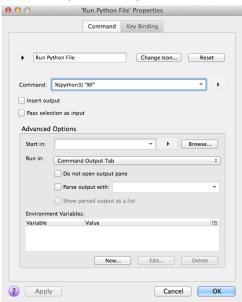
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### Komodo Run Python File Properties



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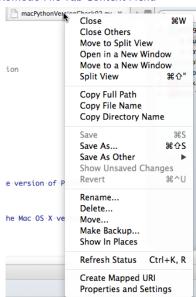
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#### Komodo File Tab Context Menu



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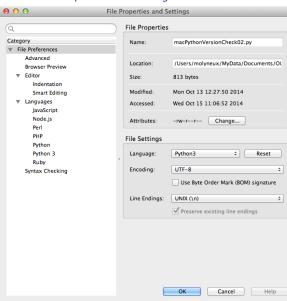
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### Komodo File Properties and Settings



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Indentation and Tabs — Questions

- How do you set spaces per indent to 2 or 4?
- How do you make the Tab key issue spaces?
- Why is the Tab character evil?

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Indentation and Tabs — Answers

► How do you set spaces per indent to 2 or 4?

► How do you make the *Tab* key issue spaces?

▶ Why is the *Tab* character *evil*?

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Indentation and Tabs — Answers

How do you set spaces per indent to 2 or 4?
Preferences... Editor Global Indentation Settings (default 8)

► How do you make the *Tab* key issue spaces?

▶ Why is the *Tab* character *evil*?

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Indentation and Tabs — Answers

- How do you set spaces per indent to 2 or 4?
  Preferences... Editor Global Indentation Settings (default 8)
- ► How do you make the *Tab* key issue spaces?

  Preferences... Editor Global Indentation Settings and uncheck

  Prefer Tab characters over spaces
- ▶ Why is the *Tab* character *evil*?

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Indentation and Tabs — Answers

How do you set spaces per indent to 2 or 4?
Preferences... Editor Global Indentation Settings (default 8)

► How do you make the *Tab* key issue spaces ?

Preferences... Editor Global Indentation Settings and uncheck

Prefer Tab characters over spaces

Why is the *Tab* character *evil*?
See Tabs vs Spaces, Tab key

- See Python Enhancement Proposals (PEP 8) Style Guide for Python Code
- Mixing tabs and spaces can lead to inconsistent layout when copying from one editor to another or MS Word
- ► Tab character is Unicode U+0009 or ^I or HT or \t see C0 and C1 control codes

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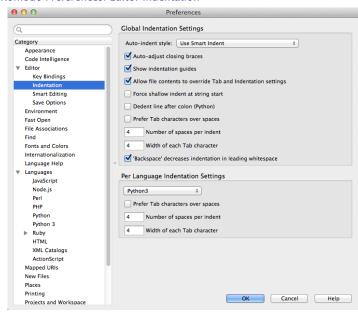
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#### Komodo Preferences: Editor Indentation



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Python Usage — Questions

- How do you enter an interactive Python shell?
- How do you exit Python in Terminal (Mac) or Command prompt (Windows)?
- How do you get help in a shell?
- How do you exit the interactive help utility?

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Python Usage — Answers

How do you enter an interactive Python shell?

How do you exit Python in Terminal (Mac) or Command prompt (Windows)?

How do you get help in a shell?

▶ How do you exit the interactive help utility?

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Python Usage — Answers

How do you enter an interactive Python shell?
Windows PythonWin Shell from Toolbox; Mac python3 in Terminal

- How do you exit Python in Terminal (Mac) or Command prompt (Windows)?
- How do you get help in a shell?
- ▶ How do you exit the interactive help utility?

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Python Usage — Answers

How do you enter an interactive Python shell?
Windows PythonWin Shell from Toolbox; Mac python3 in Terminal

How do you exit Python in Terminal (Mac) or Command prompt (Windows)?

quit()

How do you get help in a shell?

► How do you exit the *interactive help utility*?

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Python Usage — Answers

► How do you enter an interactive Python shell?

Windows PythonWin Shell from Toolbox: Mac python3 in Terminal

How do you exit Python in Terminal (Mac) or Command prompt (Windows)?

quit()

How do you get help in a shell? help()

► How do you exit the *interactive help utility*?

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► How do you enter an interactive Python shell?

Windows PythonWin Shell from Toolbox; Mac python3 in Terminal

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quit()

How do you get help in a shell? help()

How do you exit the interactive help utility?

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Sequences Indexing, Slices

- xs[i:j:k] is defined to be the sequence of items from index i to (j-1) with step k.
- If k is omitted or None, it is treated as 1.
- ▶ If i or j are negative then they are relative to the end.
- If i is omitted or None use 0.
- If j is omitted or None use len(xs)

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Haskell Example

### Given the following definitions

```
xs = [10.9, 25, "Phil", 3.14, 42, 1985]
vs = \lceil \lceil 5 \rceil \rceil * 3
```

### **Evaluate**

10

```
xs[1]
  xs[0]
   xs[5]
   ys
   xs[1:3]
  xs[::2]
  xs[1:-1]
  xs[-3]
   xs[:]
9
   ys[0].append(4)
```

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### Given the following definitions

```
xs = [10.9,25,"Phil",3.14,42,1985]
ys = [[5]] * 3
```

### **Evaluate**

```
1 xs[1]
                   == 25
2 xs[0]
                   == 10.9
                   == 1985
3 xs[5]
                   == [[5],[5],[5]]
4 ys
                   == [25, 'Phil']
5xs[1:3]
                   == [10.9, 'Phil', 42]
6xs[::2]
                   == [25, 'Phil', 3.14, 42]
7xs[1:-1]
8xs[-3]
                   == 3.14
9xs[:]
                   == [10.9, 25, 'Phil', 3.14, 42, 1985]
10ys[0].append(4) == [[5, 4], [5, 4], [5, 4]]
```

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- 1. Create *someProgram*.py with assignment statements defining variables and other data along with function definitions.
- There may be auxiliary files with other definitions (for example, Python Activity 2.2 has Stack.py with the Stack class definition) — this uses the import statement in someProgram.py

from someOtherDefinitions import someIdentifier

- 3. Load *someProgram*.py into *Komodo Edit* and use the *Run Python File* macro from the *Toolbox*
- 4. For further results, edit the file in *Komodo Edit* and and use the *Save and Run* macro from the *Toolbox*

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 In Terminal (Mac) or Command Prompt (Windows), navigate to someDefinitions.py and invoke the Python 3 interpreter

3. Load *someDefinitions*.py into *Python 3* with one of

from someDefinitions import \*

import someDefinitions as sdf

The as sdf gives a shorter qualifier for the namespace — names in the file are now sdf.x

Note that the commands are executed — any print statement will execute

4. At the *Python 3* interpreter prompt, evaluate expressions (may have side effects and alter definitions)

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1. For further results, edit the file in *Your Favourite Editor* and use one of the following commands:

```
reload(sdf)
import imp
imp.reload(sdf)
```

Note the use of the name sdf as opposed to the original name.

Read the following references about the dangers of reloading as compared to re-cycling *Python 3* 

- ► How to re import an updated package while in Python Interpreter?
- ► How do I unload (reload) a Python module?
- Reloading Python modules
- How to dynamically import and reimport a file containing definition of a global variable which may change anytime

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# **Program Complexity**

#### Big O Notation

- Measuring program complexity introduced in section 4 of M269 Unit 2
- See also Miller and Ranum chapter 2 Big-O Notation
- See also Wikipedia: Big O notation
- See also Big-O Cheat Sheet

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#### Comple

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- Complexity of algorithm measured by using some surrogate to get rough idea
- In M269 mainly using assignment statements
- For exact measure we would have to have cost of each operation, knowledge of the implementation of the programming language and the operating system it runs under.
- But mainly interested in the following questions:
- ▶ (1) Is algorithm A more efficient than algorithm B for large inputs?
- ▶ (2) Is there a lower bound on any possible algorithm for calculating this particular function?
- (3) Is it always possible to find a polynomial time  $(n^k)$  algorithm for any function that is computable
- the later questions are addressed in Unit 7

- O(log n) logarithmic binary search of sorted array, binary search tree, binomial heap operations
- ightharpoonup O(n) linear searching an unsorted list
- ► O(n log n) loglinear heapsort, quicksort (best and average), merge sort
- O(n²) quadratic bubble sort (worst case or naive implementation), Shell sort, quicksort (worst case), selection sort, insertion sort
- $\triangleright$   $O(n^c)$  polynomial
- O(c<sup>n</sup>) exponential travelling salesman problem via dynamic programming, determining if two logical statements are equivalent by brute force
- ightharpoonup O(n!) factorial TSP via brute force.

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# **Program Complexity**

Tyranny of Asymptotics

- Table from Bentley (1984, page 868)
- Cubic algorithm on Cray-1  $3.0n^3$  nanoseconds
- ▶ Linear algorithm on TRS-80  $19.5n \times 10^6$  nanoseconds

N	Cray-1	TRS-80
10	3.0 microsecs	200 millisecs
100	3.0 millisecs	2.0 secs
1000	3.0 secs	20 secs
10000	49 mins	3.2 mins
100000	35 days	32 mins
1000000	95 yrs	5.4 hrs

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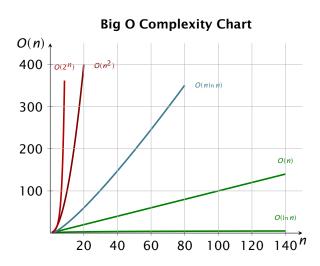
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## **Program Complexity**

Big O Complexity Chart



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- but O(g(x)) is the class of all functions h(x) such that  $|h(x)| \le C|g(x)|$  for some constant C
- ► So we should write  $f(x) \in O(g(x))$  (but we don't)
- We ought to use a notation that says that (informally) the function f is bounded both above and below by g asymptotically
- ► This would mean that for big enough x we have  $k_1 g(x) \le f(x) \le k_2 g(x)$  for some  $k_1, k_2$
- ► This is Big Theta,  $f(x) = \Theta(g(x))$
- But we use Big O to indicate an asymptotically tight bound where Big Theta might be more appropriate
- ► See Wikipedia: Big O Notation
- ► This could be Maths phobia generated confusion

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# **Program Complexity**

#### Example

```
5 def someFunction(aList) :
6    n = len(aList)
7    best = 0
8    for i in range(n) :
9     for j in range(i + 1, n + 1) :
10         s = sum(aList[i:j])
11         best = max(best, s)
12    return best
```

- Example from M269 Unit 2 page 46
- Code in file M269TutorialProgPythonADT.py
- ▶ What does the code do?
- ► (It was a *famous* problem from the late 1970s/early 1980s)
- Can we construct a more efficient algorithm for the same computational problem?

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- Described in Bentley (1984), (1988, column 7), (2000, column 7) Also in Gries (1989)
- These are all in a procedural programming style (as in C, Java, Python)
- Problem arose from medical image processing.
- ▶ A functional approach using Haskell is in Bird (1998, page 134), (2014, page 127, 133) a variant on this called the *Not the maximum segment sum* is given in Bird (2010, Page 73) both of these *derive* a linear time program from the (*n*<sup>3</sup>) initial specification
- See Wikipedia: Maximum subarray problem
- ► See Rosetta Code: Greatest subsequential sum

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## **Program Complexity**

Example (3)

- Here is the same program but modified to allow lists that may only have negative numbers
- ▶ The complexity T(n) function will be slightly different
- but the Big O complexity will be the same

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- ► Complexity function T(n) for maxSubSeg01()
- Two initial assignments
- ▶ The outer loop will be executed (n-1) times,
- ► Hence the inner loop is executed

$$(n-1) + (n-2) + ... + 2 + 1 = \frac{(n-1)}{2} \times n$$

Assume sum() takes n assignments

► Hence 
$$T(n) = 2 + (n+2) \times \left(\frac{(n-1)}{2} \times n\right)$$
  

$$= 2 + (n+2) \times \left(\frac{n^2}{2} - \frac{n}{2}\right)$$

$$= 2 + \frac{1}{2}n^3 - \frac{1}{2}n^2 + n^2 - n$$

$$= \frac{1}{2}n^3 + \frac{1}{2}n^2 - n + 2$$

 $\blacktriangleright \text{ Hence } O(n^3)$ 

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## **Program Complexity**

Example (5)

- Developing a better algorithm
- Assume we know the solution (maxSoFar) for xs[0..(i 1)]
- ▶ We extend the solution to xs[0..i] as follows:
- The maximum segment will be either maxSoFar
- or the sum of a sublist ending at i (maxToHere) if it is bigger
- ► This reasoning is similar to divide and conquer in binary search or Dynamic programming (see Unit 5)
- Keep track of both maxSoFar and maxToHere the Eureka step

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```
27 def maxSubSeg02(xs) :
28  maxToHere = xs[0]
29  maxSoFar = xs[0]
30  for x in xs[1:] :
31  # Invariant: maxToHere, maxSoFar OK for xs[0..(i-1)]
32  maxToHere = max(x, maxToHere + x)
33  maxSoFar = max(maxSoFar, maxToHere)
34  return maxSoFar
```

- ► Complexity function T(n) = 2 + 2n
- ► Hence *O*(*n*)
- ▶ What if we want more information?
- Return the (or a) segment with max sum and position in list

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```
38 def maxSubSeq03(xs) :
    maxSoFar = maxToHere = xs[0]
    startIdx, endIdx, startMaxToHere = 0, 0, 0
    for i. x in enumerate(xs) :
41
      if maxToHere + x < x:
42
        maxToHere = x
43
        startMaxToHere = i
44
45
      else ·
        maxToHere = maxToHere + x
46
      if maxSoFar < maxToHere :</pre>
48
        maxSoFar = maxToHere
49
        startIdx, endIdx = startMaxToHere, i
50
    return (maxSoFar.xs[startIdx:endIdx+1].startIdx.endIdx)
52
```

- Developing a better algorithm maxSubSeg03()
- Complexity function worst case T(n) = 2 + 3 + (2 + 3)n
- ► Hence still *O*(*n*)
- ► Note Python assignments, enumerate() and tuple

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Example (8)

Sample data and output

```
56egList = [-2,1,-3,4,-1,2,1,-5,4]

58egList01 = [-1,-1,-1]

60 egList02 = [1,2,3]

62 assert maxSubSeg03(egList) == (6, [4, -1, 2, 1], 3, 6)

64 assert maxSubSeg03(egList01) == (-1, [-1], 0, 0)

66 assert maxSubSeg03(egList02) == (7, [1, 2, 3], 0, 2)
```

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### **Program Complexity**

Python Data Types — Lists

Operation	Notation	Average	Amortized Worst
Get item	x = xs[i]	O(1)	O(1)
Set item	xs[i] = x	<b>O</b> (1)	<b>O</b> (1)
Append	XS = YS + ZS	<b>O</b> (1)	<b>O</b> (1)
Сору	xs = ys[:]	O(n)	O(n)
Pop last	xs.pop()	O(1)	<b>O</b> (1)
Pop other	xs.pop(i)	O(k)	O(k)
Insert(i,x)	xs[i:i] = [x]	O(n)	O(n)
Delete item	del xs[i:i+1]	O(n)	O(n)
Get slice	xs = ys[i:i]	O(k)	O(k)
Set slice	xs[i:i] = vs	O(k+n)	O(k+n)
Delete slice	xs[i:j] = []	O(n)	O(n)
Member	x in xs	O(n)	
Get length	n = len(xs)	<b>O</b> (1)	<b>O</b> (1)
Count(x)	n = xs.count(x)	O(n)	O(n)

- Source https://wiki.python.org/moin/TimeComplexity
- See https://docs.python.org/3/library/stdtypes.html# sequence-types-list-tuple-range

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£....

## **Program Complexity**

User Defined Type — Bags

```
sclass Bag:
    def __init__(self):
      self.list = []
8
10
    def add(self. item):
      self.list.append(item)
11
    def remove(self. item):
13
      self.list.remove(item)
14
    def contains(self. item):
16
      return item in self.list
17
    def count(self. item):
19
      return self.list.count(item)
20
    def size(self):
22
      return len(self.list)
23
    def __str__(self):
25
      return str(self.list)
26
```

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# Using a Data Type

Information Retrieval Functions

- Term Frequency, tf, takes a string, term, and a Bag. document
  - returns occurrences of term divided by total strings in document
- Inverse Document Frequency, idf, takes a string, term, and a list of Bags, documents returns  $\log(\text{total}/(1 + \text{containing}))$  — total is total number of Bags, containing is the number of Bags containing term
- tf-idf, tf\_idf, takes a string, term, and a list of Bags, documents

```
returns a sequence [r_0, r_1, \dots, r_{n-1}] such that
r_i = \mathsf{tf}(\mathsf{term}, d_i) \times \mathsf{idf}(\mathsf{term}, \mathsf{documents})
```

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- **Exponential function**  $y = a^x$  or  $f(x) = a^x$
- $a^n = a \times a \times \cdots \times a$  (n a terms)
- ► Logarithm reverses the operation of exponentiation
- $\triangleright \log_a y = x \text{ means } a^x = y$
- $\log_a 1 = 0$
- $\triangleright \log_a a = 1$
- Method of logarithms propounded by John Napier from 1614
- Log Tables from 1617 by Henry Briggs
- Slide Rule from about 1620-1630 by William Oughtred of Cambridge
- Logarithm from Greek logos ratio, and arithmos number (Chanbers Dictionary 13th edition 2014)

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2. 
$$a^m \div a^n = a^{m-n}$$

3. 
$$a^{-m} = \frac{1}{a^m}$$

4. 
$$a^{\frac{1}{m}} = \sqrt[m]{a}$$

5. 
$$(a^m)^n = a^{mn}$$

6. 
$$a^{\frac{n}{m}} = \sqrt[m]{a^n}$$

7. 
$$a^0 = 1$$
 where  $a \neq 0$ 

- **Exercise** Justify the above rules
- ► What should 0<sup>0</sup> evaluate to?
- ► See Wikipedia: Exponentiation
- ► The justification above probably only worked for whole or rational numbers see later for exponents with real numbers (and the value of logarithms, calculus...)

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#### Motivation

- Make arithmetic easier turns multiplication and division into addition and subtraction (see later)
- Complete the range of elementary functions for differentiation and integration
- An elementary function is a function of one variable which is the composition of a finite number of arithmetic operations  $((+), (-), (\times), (\div))$ , exponentials, logarithms, constants, and solutions of algebraic equations (a generalization of nth roots).
- The elementary functions include the trigonometric and hyperbolic functions and their inverses, as they are expressible with complex exponentials and logarithms.
- ► See A Level FP2 for Euler's relation  $e^{i\theta} = \cos \theta + i \sin \theta$
- ► In A Level C3, C4 we get  $\int \frac{1}{x} = \log_e |x| + C$
- e is Fuler's number 2.71828...

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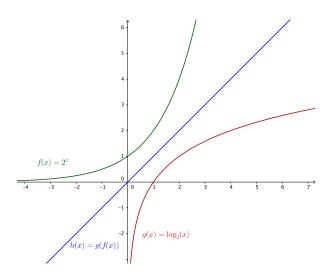
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## **Exponentials and Logarithms**

#### Graphs

See GeoGebra file expLog.ggb



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# **Exponentials and Logarithms**

Laws of Logarithms

- ► Multiplication law  $\log_a xy = \log_a x + \log_a y$
- **Division law**  $\log_a \left( \frac{x}{y} \right) = \log_a x \log_a y$
- **Power law**  $\log_a x^k = k \log_a x$
- Proof of Multiplication Law

$$x = a^{\log_a x}$$
 $y = a^{\log_a y}$  by definition of log
 $xy = a^{\log_a x} a^{\log_a y}$ 
 $= a^{\log_a x + \log_a y}$  by laws of indices
Hence  $\log_a xy = \log_a x + \log_a y$  by definition of log

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- ▶ Addition add(b, x) = x + b
- **Subtraction** sub(b, x) = x b
- Inverse sub(b, add(b, x)) = (x + b) b = x
- ▶ Multiplication  $mul(b, x) = x \times b$
- **Division**  $div(b, x) = x \div b = \frac{x}{b} = x/b$
- ► Inverse div(b, mul(b, x)) =  $(x \times b) \div b = \frac{(x \times b)}{b} = x$
- **Exponentiation**  $exp(b, x) = b^x$
- **Logarithm**  $\log(b, x) = \log_b x$
- Inverse  $\log(b, \exp(b, x)) = \log_b(b^x) = x$
- What properties do the operations have that work (or not) with the notation?

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- **Associativity**  $(x \circledast y) \circledast z = x \circledast (y \circledast z)$
- ► (+) and (×) are *semantically* commutative and associative so we can leave the brackets out
- ► (-) and (÷) are not
- ► Evaluate (3 (2 1)) and ((3 2) 1)
- Evaluate (3/(2/2)) and ((3/2)/2)
- We have the syntactic ideas of left (and right) associativity
- ▶ We choose (-) and (÷) to be left associative
- ightharpoonup 3 2 1 means ((3 2) 1)
- ► 3/2/2 means ((3/2)/2)
- Operator precedence is also a choice (remember BIDMAS or BODMAS ?)
- If in doubt, put the brackets in

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## **Exponentials and Logarithms**

#### **Associativity**

- ► What should 2<sup>34</sup> mean?
- Let  $b \wedge x \equiv b^x$
- Evaluate (2 ^ 3) ^ 4 and 2 ^ (3 ^ 4)
- Evaluate  $c = \log_b(\log_b((b \land b) \land x))$
- Evaluate  $d = \log_b(\log_b(b \land (b \land x)))$
- Beware spreadsheets Excel and LibreOffice here

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- $(2^3)^4 = 2^{12}$  and  $2^{3^4} = 2^{81}$
- Exponentiation is not semantically associative
- ► We *choose* the syntactic left or right associativity to make the syntax nicer.
- Evaluate  $c = \log_b(\log_b((b \land b) \land x))$
- $c = \log_b(x \log_b(b^b)) = \log_b(x \cdot (b \log_b b)) = \log_b(x \cdot b \cdot 1)$
- $\blacktriangleright \text{ Hence } c = \log_b x + \log_b b = \log_b x + 1$
- Not symmetrical (unless *b* and *x* are both 2)
- Evaluate  $d = \log_b(\log_b(b \land (b \land x)))$
- $d = \log_b((b \land x)(\log_b b)) = \log_b((b \land x) \times 1)$
- $\qquad \qquad \mathsf{Hence} \ d = \log_b(b \land x) = x(\log_b b) = x$
- ▶ Which is what we want so exponentiation is *chosen* to be right associative

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### ► Change of base

$$\log_{a} x = \frac{\log_{b} x}{\log_{b} a}$$
**Proof:** Let  $y = \log_{a} x$ 

$$a^{y} = x$$

$$\log_{b} a^{y} = \log_{b} x$$

$$y \log_{b} a = \log_{b} x$$

$$y = \frac{\log_{b} x}{\log_{b} a}$$

• Given x,  $\log_b x$ , find the base b

$$b = x^{\frac{1}{\log_b x}}$$

$$b = x^{\log_b x}$$

$$\log_a b = \frac{1}{\log_b a}$$

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## **Before Calculators and Computers**

- We had computers before 1950 they were humans with pencil, paper and some further aids:
- Slide rule invented by William Oughtred in the 1620s major calculating tool until pocket calculators in 1970s
- Log tables in use from early 1600s method of logarithms propounded by John Napier
- Logarithm from Greek logos ratio, and arithmos number

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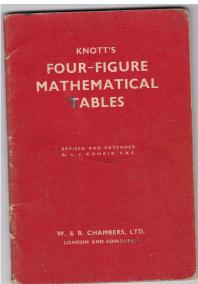
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## **Log Tables**

Knott's Four-Figure Mathematical Tables



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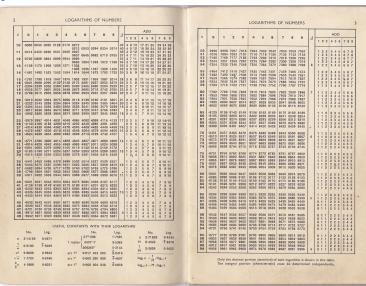
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## Log Tables

#### Logarithms of Numbers



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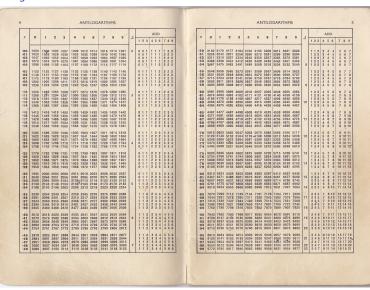
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## Log Tables

### **Antilogarithms**



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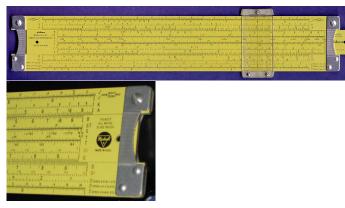
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### Slide Rules

Pickett N 3-ES from 1967



- See Oughtred Society
- ▶ UKSRC
- ► Rod Lovett's Slide Rules
- ► Slide Rule Museum

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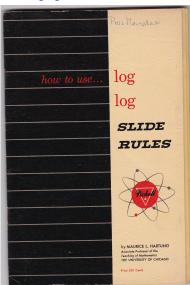
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### Slide Rules

### Pickett log log Slide Rules Manual 1953



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### **Calculators**

HP HP-21 Calculator from 1975 £69



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### **Calculators**

Casio fx-85GT PLUS Calculator from 2013 £10



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### Calculators

#### Calculator Links

- ► **HP Calculator Museum** http://www.hpmuseum.org
- HP Calculator Emulators http://nonpareil.brouhaha.com
- ► HP Calculator Emulators for OS X http://www.bartosiak.org/nonpareil/
- ► Vintage Calculators Web Museum http://www.vintagecalculators.com

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- ► Evaluate 89.7 × 597
- Knott's Tables
- $ightharpoonup \log_{10} 89.7 = 1.9528 \text{ and } \log_{10} 597 = 2.7760$
- Shows mantissa (decimal) & characteristic (integral)
- Add 4.7288, take *antilog* to get  $5346 + 10 = 5.356 \times 10^4$
- HP-21 Calculator set display to 4 decimal places
- $\triangleright$  89.7  $\log$  = 1.9528 and 597  $\log$  = 2.7760
- + displays 4.7288
- ► 10 ENTER,  $x \neq y$  and  $y^x$  displays 53550.9000
- Casio fx-85GT PLUS
- log 89.7 ) = 1.952792443 + log 597 ) = 2.775974331 =
- 4.728766774 Ans + 10x gives 53550.9

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Haskell Example

- Vehicles should not wait on red on BD for too long.
- ► If there is a long queue on AC then BD is only given a green for a short interval.
- If both queues are long the usual flow times are used.
- We use the following propositions:
  - w Vehicles have been waiting on red on BD for too long
  - q Queue on AC is too long
  - r Queue on BD is too long
- Given the following events:
  - ► ToBD Change flow to BD
  - ► ToBDShort Change flow to *BD* for short time
  - NoChange No Change to lights
- Express above as truth table, outcome tree, boolean expression

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Haskell Example

Traffic Lights Example (2)

### Traffic Lights outcome table

W	q	r	Event
T T T F	T T F F T	T F T F	ToBD ToBDSort ToBD ToBD NoChange NoChange
F F	F F	T F	NoChange NoChange

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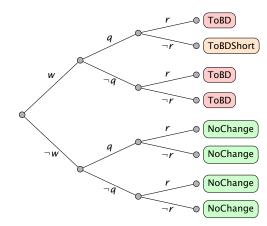
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Traffic Lights Example (3)

### ► Traffic lights outcome tree



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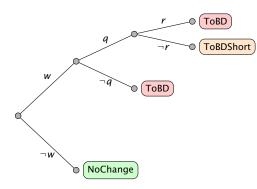
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Traffic Lights Example (4)

Traffic lights outcome tree simplified



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Haskell Example

Traffic Lights Example (5)

- Traffic Lights code 01
- See M269TutorialProgPythonADT01.py

```
3def trafficLights01(w,q,r) :
    Input 3 Booleans
    Return Event string
    if w:
      if a:
9
        if r:
10
          evnt = "ToBD"
11
        else:
          evnt = "ToBDShort"
13
      else:
14
        evnt = "ToBD"
15
    else:
16
      evnt = "NoChange"
17
18
    return evnt
```

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Haskell Example

Traffic Lights Example (6)

### ► Traffic Lights test code 01

```
22 trafficLights01Evnts = [((w,q,r), trafficLights01(w,q,r))
                                 for w in [True.False]
23
                                 for q in [True, False]
24
                                 for r in [True.False]]
25
27 assert trafficLights01Evnts \
    == [((True, True, True), 'ToBD')
28
         ((True, True, False), 'ToBDShort')
29
30
         ((True, False, True), 'ToBD')
         ,((True, False, False), 'ToBD')
31
         ((False, True, True), 'NoChange')
32
         .((False. True. False).
                                  'NoChange')
33
         .((False, False, True), 'NoChange')
34
         ((False, False, False), 'NoChange')]
35
```

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Haskell Example

Traffic Lights Example (7)

► Traffic Lights code 02 compound Boolean conditions

```
37 def trafficLights02(w,q,r) :
38
    Input 3 Booleans
39
    Return Event string
41
    if ((w and q and r) or (w and not q)):
42
      evnt = "ToBD"
43
    elif (w and q and not r):
45
      evnt = "ToBDShort"
    else:
46
      evnt = "NoChange"
47
    return evnt
48
```

What objectives do we have for our code?

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Traffic Lights Example (8)

### ► Traffic Lights test code 02

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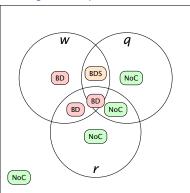
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Traffic Lights Example (9)



- Traffic Lights Venn diagram
- OK using a fill colour would look better but didn't have the time to hack the package

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Haskell Example

Validity

- Validity of Boolean expressions
- Complete every outcome returns an event (or error message, raises an exception)
- Consistent we do not want two nested if statements or expressions resulting in different events
- We check this by ensuring that the events form a disjoint partition of the set of outcomes — see the Venn diagram
- We would quite the programming language processor to warn us otherwise — not always possible

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Truth Function

Haskell Example

- c Rail card
- q Off-peak time
- s Special offer
- 4 fares: Standard, Reduced, Special, Super Special
- ► Rules:
  - 1. Reduced fare if rail card or at off-peak time
  - Without rail card no reduction for both special offer and off-peak.
  - Rail card always has reduced fare but cannot get off-peak discount as well.
  - Rail card gets super special discount for journey with special offer
- Draw up truth table, outcome tree, Venn diagram and conditional statement (or expression) for this

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Haskell Example

Rail Ticket Exercise (2)

Rail ticket outcome table

С	q	S	Event			
T T T F F	T F F T F	T F T F T	Super Special Reduced Super Special Reduced Special Reduced Special			
F	F	F	Standard			

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Haskell Example

- Rail ticket outcome table
- Note that it may be more convenient to change columns

С	s	q	Event		
T T T F F	T F	T F T F T	Super Special Super Special Reduced Reduced Special Special Reduced		
F	F	F	Standard		

► Real fares are a little more complex — see brfares.com

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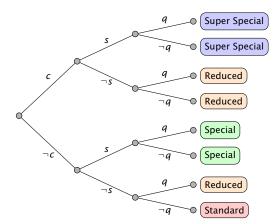
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Rail Ticket Exercise (4)

#### Rail Ticket outcome tree



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#### Boolean Expressions Exercise

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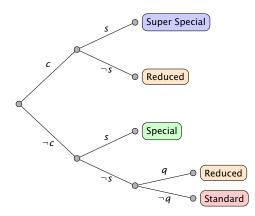
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Rail Ticket Exercise (5)

Rail Ticket outcome tree simplified



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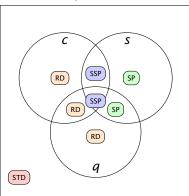
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Rail Ticket Example (6)



► Rail Ticket Venn diagram

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Haskell Example

Rail Ticket Example (7)

#### ► Rail Ticket code 01

```
61 def railTicket01(c,s,q):
62
    Input 3 Booleans
63
    Return Event string
65
    if c:
66
      if s:
67
        evnt = "SSP"
69
      else:
        evnt = "RD"
70
    else:
71
      if s:
72
        evnt = "SP"
73
      else:
74
        if q:
75
          evnt = "RD"
76
77
        else:
          evnt = "STD"
78
79
    return evnt
```

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Rail Ticket Example (8)

#### ► Rail Ticket test code 01

```
83 railTicket01Evnts = [((c,s,q), railTicket01(c,s,q))
                                 for c in [True, False]
84
                                 for s in [True, False]
85
                                 for a in [True.False]]
86
88 assert railTicket01Evnts \
    == [((True, True, True), 'SSP')
         ,((True, True, False), 'SSP')
90
91
         ((True, False, True), 'RD')
         .((True. False. False).
                                  'RD')
92
                                 'SP')
         ((False, True, True),
93
         .((False, True, False).
         .((False, False, True), 'RD')
95
         ((False, False, False), 'STD')]
96
```

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▶ Rail Ticket code 02 compound Boolean expressions

```
98 def railTicket02(c,s,q):
99
     Input 3 Booleans
100
    Return Event string
101
102
     if (c and s):
       evnt = "SSP"
104
    elif ((c and not s) or (not c and not s and q)) :
105
       evnt = "RD"
106
    elif (not c and s):
107
       evnt = "SP"
108
    else:
109
       evnt = "STD"
110
111
    return evnt
```

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Rail Ticket Example (10)

#### Rail Ticket test code 02

120 assert railTicket02Evnts == railTicket01Evnts

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## **Propositional Calculus**

#### Introduction

- Unit 2 section 3.2 A taste of formal logic introduces Propositional calculus
- A language for calculating about Booleans truth values
- ► Gives operators (connectives) conjunction (∧) AND, disjunction (∨) OR, negation (¬) NOT, implication (⇒) IF
- ► There are 16 possible functions  $(\mathbb{B}, \mathbb{B}) \to \mathbb{B}$  see below defined by their truth tables
- ▶ **Discussion** Did you find the truth table for implication weird or surprising?

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#### **Implication**

- ► Implication has a negative definition we accept its truth unless we have contrary evidence
- $T \Rightarrow T == T \text{ and } T \Rightarrow F == F$
- Hence 4 possibilities for truth table

p	q	$b \Leftrightarrow d$	ь	$b \Leftrightarrow d$	$b \lor d$
Т	Т	Т	Т	Т	Т
Т	F	F	F	F	F
F	Т	Т	Т	F	F
F	F	Т	F	Т	F

- ightharpoonup ( $\Rightarrow$ ) must have the entry shown the others are taken
- Do not think of p causing q

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# **Propositional Calculus**

Functional Completeness, Boolean Programming

- Functionally complete set of connectives is one which can be used to express all possible connectives
- ▶  $p \Rightarrow q \equiv \neg p \lor q$  so we could just use  $\{\neg, \land, \lor\}$
- Boolean programming we have to have a functionally complete set but choose more to make the programming easier
- Expressiveness is an issue in programming language design

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- ▶ NAND  $p\overline{\wedge}q$ ,  $p \uparrow q$ , Sheffer stroke
- ▶ NOR  $p \overline{\lor} q$ ,  $p \downarrow q$ , Pierce's arrow
- See truth tables below both {↑}, {↓} are functionally complete
- **Exercise** verify
  - $\neg p \equiv p \uparrow p$

  - $\neg p \equiv p \downarrow p$
- Not a novelty the Apollo Guidance Computer was implemented in NOR gates alone.

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#### **Truth Function References**

- The following appendix notes illustrate the 16 binary functions of two Boolean variables
- ► See Truth function
- ► See Functional completeness
- ► See Sheffer stroke
- ► See Logical NOR

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#### **Table of Binary Truth Functions**

p	q	Т	<b>b</b> \ \ <b>d</b>	$b \Rightarrow d$	þ	$b \Leftrightarrow d$	ь	$b \Leftrightarrow d$	<b>b</b> < <b>d</b>
T T F	T F T F	T T T	T T T F	T T F T	T T F	T F T T	T F T F	T F F T	T F F
р	q	1	<b>b</b> <u>\</u> d	<b>b</b> \$ <b>d</b>	ď	<b>b</b> ⇔ <b>d</b>	<b>b</b> [	b	<b>b</b> × <b>d</b>
Т	Т	F	F	F	F	F	F	F T	F T

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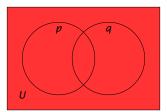
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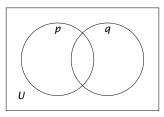
Truth Function

Tautology/Contradiction

**► Tautology** True, ⊤, *Top* 



**► Contradiction** False, ⊥, *Bottom* 



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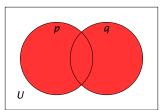
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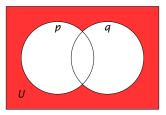
Haskell Example

Disjunction/Joint Denial

**Disjunction** OR,  $p \vee q$ 



▶ **Joint Denial NOR**,  $p\overline{\lor}q$ ,  $p\downarrow q$ , *Pierce's arrow* 



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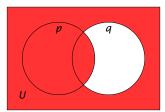
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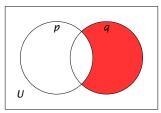
Haskell Example

Converse Implication/Converse Nonimplication

**Converse Implication**  $p \in q$ 



**Converse Nonimplication**  $p \notin q$ 



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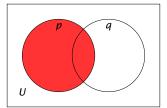
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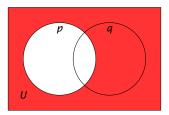
Haskell Example

Proposition p/Negation of p

#### $\triangleright$ Proposition p



#### $\triangleright$ Negation of p



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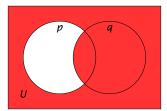
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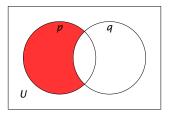
Haskell Example

Material Implication/Material Nonimplication

▶ Material Implication  $p \Rightarrow q$ 



► Material Nonimplication  $p \Rightarrow q$ 



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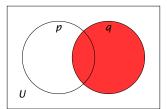
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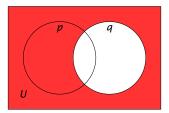
Haskell Example

Proposition q/Negation of q

Proposition q q



▶ Negation of  $q \neg q$ 



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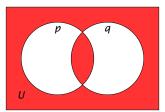
ADTs

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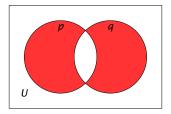
Haskell Example

#### Biconditional/Exclusive disjunction

**Biconditional** If and only if, IFF,  $p \Leftrightarrow q$ 



**Exclusive disjunction** XOR,  $p \neq q$ 



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Boolean Expressions Exercise Propositional Calculus

Truth Function

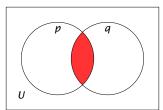
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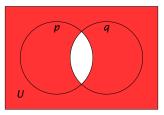
Haskell Example

Conjunction/Alternative denial

**Conjunction** AND,  $p \land q$ 



▶ Alternative denial NAND,  $p \times q$ ,  $p \uparrow q$ , Sheffer stroke



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# **Abstract Data Types**

Overview

Abstract data type is a type with associated operations, but whose representation is hidden (or not accessible)

 Common examples in most programming languages are Integer and Characters and other built in types such as tuples and lists

- Abstract data types are modeled on Algebraic structures
  - A set of values
  - Collection of operations on the values
  - Axioms for the operations may be specified as equations or pre and post conditions
- Health Warning different languages provide different ways of doing data abstraction with similar names that may mean subtly different things

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M269 Python,

- Abstract Data Types and Object-Oriented **Programming**
- Example: Shape with Circles, Squares, ... and operations draw, moveTo, ...
- ▶ ADT approach centres on the data type that tells you what shapes exist
- For each operation on shapes, you describe what they do for different shapes.
- **OO** you declare that to be a shape, you have to have some operations (draw, moveTo)
- For each kind of shape you provide an implementation of the operations
- OO easier to answer What is a circle? and add new shapes
- ADT easier to answer How do you draw a shape? and add new operations

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Haskell Example

- Health Warning and Optional Material Discussions about the merits of Functional programming and Object-oriented programming tend to look like the disputes between Lilliput and Blefuscu
- Abstract data type article contrasts ADT and OO as algebra compared to co-algebra
- What does coalgebra mean in the context of programming? is a fairly technical but accessible article.
- ► What does the *forall* keyword in Haskell do? is an accessible article on *Existential Quantification*
- ► Bart Jacobs Coalgebra
- nLab Coalgebra
- ► Beware the distinction between *concepts* and *features* in programming languages see OOP Disaster
- ▶ Not for this session this slide is here just in case

```
data Shape
      = Circle Point Radius
       | Square Point Size
3
   draw :: Shape -> Pict
   draw (Circle p r) = drawCircle p r
   draw (Square p s) = drawRectangle p s s
   moveTo :: Point -> Shape -> Shape
   moveTo p2 (Circle p1 r) = Circle p2 r
10
   moveTo p2 (Square p1 s) = Square p2 s
11
   shapes :: [Shape]
13
    shapes = [Circle (0,0) 1, Square (1,1) 2]
14
16
    shapes01 :: [Shape]
    shapes01 = map (moveTo (2,2)) shapes
17
```

 Example based on Lennart Augustsson email of 23 June 2005 on Haskell list M269 Python, Logic, ADTs

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Queue **Future Work** 

Haskell Example

```
class IsShape shape where
      draw :: shape -> Pict
2
      moveTo :: Point -> shape -> shape
3
   data Shape = forall a . (IsShape a) => Shape a
   data Circle = Circle Point Radius
    instance IsShape Circle where
      draw (Circle p r) = drawCircle p r
9
      moveTo p2 (Circle p1 r) = Circle p2 r
10
   data Square = Square Point Size
12
    instance IsShape Square where
13
      draw (Square p s) = drawRectangle p s s
14
      moveTo p2 (Square p1 s) = Square p2 s
15
   shapes :: [Shape]
17
    shapes = [Shape (Circle (0,0) 10), Shape (Square (1,1) 2)]
18
   shapes01 :: [Shape]
20
    shapes01 = map (moveShapeTo (2,2)) shapes
21
               where
22
               moveShapeTo p (Shape s) = Shape (moveTo p s)
23
```

# Abstract Data Type

Queue

- Queue Abstract Data Type operations
- makeEmptyQ returns empty queue
- ▶ isEmptyQ takes queue, returns Boolean
- addToQ takes queue, item, returns queue with item added at back
- headOfQ takes queue, returns item at front
- tailofQ takes queue, returns queue without front item
- Other operations
- removeFrontQ takes queue, returns pair of item on the front and queue with item removed
- sizeQ to save calculating it
- ▶ isFullQ for a bounded queue

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# Abstract Data Type

Queue (2)

- Pre, Post Conditions, Axioms should be complete
- They define all permissable inputs to the functions (or methods)
- They define the outcome of all applications of the functions
- Composition of the functions constructs all possible members of the ADT set

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Haskell Example
References

- Pre-conditions, Post-conditions, Axioms
- makeEmptyQ()
- ► Pre True
- Post Return value q is an empty queue
- Axiom makeEmptyQ() == EmptyQ
- ▶ isEmptyQ()
- ► Pre True
- ▶ **Post** Returns True if q is empty, otherwise False
- Axiom isEmptyQ(makeEmptyQ()) == True
- ▶ isEmptyQ(addToQ(q,x)) == False
- **Exercise** complete this for the other operations

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Haskell Example

- ► addToQ()
- ▶ Pre True
- ► **Post** Returns queue with x at back, front part is input queue
- ► headOfQ()
- Pre Argument q is non-empty
- Post Return value is item at the front (queue is unchanged)
- Axioms headOfQ(makeEmptyQ()) == error
- ▶ headOfQ(addToQ(makeEmptyQ(),x)) == x
- ▶ headOfQ(addToQ(q,x)) == headOfQ(q)

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Haskell Example

- Pre-conditions, Post-conditions, Axioms
- ► tail0fQ()
- ▶ Pre True
- ▶ Post Returns queue without first item
- Axioms tailofQ(makeEmptyQ()) == error
- ▶ tailOfQ(addToQ(makeEmptyQ(),x)) == EmptyQ
- ► tailOfQ(addToQ(q,x)) == addToQ(tailOfQ(q),x)

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Haskell Example References

## Abstract Data Type

Queue Implementation (1)

- Queue Implementation
- Using Lists as Queues section 5.1.2 of the Tutorial
- ▶ Quote: It is also possible to use a list as a queue, where the first element added is the first element retrieved (first-in, first-out); however, lists are not efficient for this purpose. While appends and pops from the end of list are fast, doing inserts or pops from the beginning of a list is slow (because all of the other elements have to be shifted by one).
- ► Could use collections.deque but we will use a pair of lists See Okasaki (1998, page 42)

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### Abstract Data Type

Queue Implementation (2)

- Queue Implementation 1
- Using a namedtuple()
- A factory function for creating tuple subclasses with named fields

```
5 from collections import namedtuple
7Qp1 = namedtuple('Qp1',['frs','rbks'])
```

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## Queue Implementation 1 main operations

```
9def makeEmptyQp1():
   return 0p1([],[])
12 def isEmptyQp1(q):
   return a.frs == []
15 def addToOp1(q.x):
   return checkQp1(q.frs, [x] + q.rbks[:])
18 def headOfOp1(q):
   if q.frs == [] :
      RunTimeError("headOfOp1 applied to empty queue")
    else:
21
      return q.frs[0]
22
24 def tailOfOp1(q):
    if q.frs == [] :
      RunTimeError("tailOfOp1 applied to empty queue")
    else:
27
      return checkQp1(q.frs[1:], q.rbks[:])
28
```

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Haskell Example
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Queue Implementation 1 checkOp1()

```
30 def checkQp1(frs, rbks):
31    if frs == [] :
32        bks = rbks[:]
33        bks.reverse()
34        return Qp1(bks, [])
35    else :
36    return Qp1(frs, rbks)
```

- ▶ Note copying of arguments see below for reason
- Note also in stringQp1Items below at line 47 on slide 151
- ▶ implicit line joining using (()) (why is this needed ??)
- Note use of recursion

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Haskell Example

- Functions, Immutable and Mutable Arguments
- Immutable arguments are passed by value
- Mutable arguments are passed by reference
- Immutable: numbers, strings, tuples
- Mutable: Lists, dictionaries, sets, and most objects in user classes

```
>>> def changer (a,b):
... a = 2
... b[0] = 'spam'
...
>>> n = 1
>>> xs = [1,2]
>>> changer(n, xs)
>>> (n,xs)
(1, ['spam', 2])
```

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Haskell Example

## Queue Implementation 1 conversion operations

```
38 def stringQp1(q) :
   return ("<" + stringQp1Items(q) + ">")
41 def stringOp1Items(q) :
   if isEmptyQp1(q) :
      return
43
   elif isEmptvOp1(tailOfOp1(q)) :
      return str(headOfQp1(q))
45
46
   else:
      return ( str(headOfOp1(q))
47
              + ", " + stringQp1Items(tailOfQp1(q)))
48
50 def buildOp1(xs.a) :
   if xs == []:
      return a
52
53
   else:
54
      return buildQp1(xs[1:],addToQp1(q,xs[0]))
56 def listToQp1(xs) :
57 return buildQp1(xs, makeEmptyQp1())
```

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Haskell Example

### Queue Implementation 1 test code

```
61q11 = listToQp1([1,2,3,1])
63q12 = tailOfQp1(q11)
65 assert q11 == Qp1(frs=[1], rbks=[1, 3, 2])
67 assert stringQp1(q11) == '<1,_2,_3,_1>'
69 assert q12 == Qp1(frs=[2, 3, 1], rbks=[])
71 assert stringQp1(q12) == '<2,_3,_1>'
```

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Haskell Example
References

- Queue Implementation 2
- Modify to add size
- Store in tuple to save calculating each time

```
75 Qp2 = namedtuple('Qp2',['frs','rbks','sz'])
```

**Exercise** Add size() operation and other modifications

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### Queue Implementation 2 main operations

```
77 def makeEmptyQp2():
   return 0p2([],[], 0)
80 def isEmptvOp2(a):
   return a.frs == []
83 def addToOp2(q.x):
   return checkQp2(q.frs, [x] + q.rbks[:], q.sz + 1)
86 def headOfOp2(q):
   if q.frs == [] :
      RunTimeError("headOfOp2 applied to empty queue")
    else:
89
      return q.frs[0]
90
92 def tail0f0p2(q):
    if q.frs == [] :
      RunTimeError("tailOfOp2 applied to empty queue")
    else:
95
      return checkQp2(q.frs[1:], q.rbks[:], q.sz - 1)
96
```

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Queue Implementation 2 sizeQp2(), check0p1()

```
98 def sizeOfQp2(q):
99    return q.sz

101 def checkQp2(frs, rbks, sz):
102    if frs == []:
103        bks = rbks[:]
104        bks.reverse()
105        return Qp2(bks, [], sz)
106    else:
107    return Qp2(frs, rbks, sz)
```

- Note also in stringQp2Items below at line 118 on slide 156
- ▶ implicit line joining using (()) (why is this needed ??)
- Note use of recursion

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```
109 def stringQp2(q) :
    return ("<" + stringQp2Items(q) + ">")
112 def stringOp2Items(a) :
     if isEmptyQp2(q) :
       return
114
     elif isEmptvOp2(tailOfOp2(q)) :
115
       return str(headOfQp2(q))
116
117
     else:
       return ( str(head0f0p2(q))
118
                + ", " + stringQp2Items(tailOfQp2(q)))
119
121 \operatorname{def} \operatorname{build0p2}(xs.a):
    if xs == []:
122
       return a
123
124
     else:
125
       return buildQp2(xs[1:],addToQp2(q,xs[0]))
127 def listToQp2(xs) :
return buildQp2(xs, makeEmptyQp2())
```

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Haskell Example

### ▶ Queue Implementation 2 test code

```
132 q21 = listToQp2([1,2,3,1])
134 q22 = tailOfQp2(q21)
136 assert q21 == Qp2(frs=[1], rbks=[1, 3, 2], sz=4)
138 assert stringQp2(q21) == '<1,_2,_3,_1>'
140 assert q22 == Qp2(frs=[2, 3, 1], rbks=[], sz=3)
142 assert stringQp2(q22) == '<2,_3,_1>'
```

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Inductive data type definitions

A *list* is either an empty list or a first item followed by the rest of the list

 A binary tree is either an empty tree or a node with an item and two sub-trees

Recursive definitions often easier to find than iterative

Unit 3 Sorting

Unit 4 Searching

Both use binary tree structure

See Sorting Tutorial

See Binary Trees Tutorial

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Haskell Example

### **Future Work**

#### Dates

- 2 December 2020 TMA01
- ► Saturday 5 December 2020 Tutorial Online 10:00–12:00
- 2 January 2021 Unit 4
- ► 6 January 2021 iCMA43
- ▶ 30 January 2021 Unit 5
- 3 February 2021 iCMA44
- Sunday 28 February 2021 Tutorial Online 10:00-11:00
- ▶ 6 March 2021 Unit 6
- ▶ 10 March 2021 iCMA45
- Saturday 13 March 2021 Tutorial Online 10:00–13:00

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Haskell Example

Binary Search — Haskell

The notes following give two implementations of Binary Search in Haskell

- Note: these are not part of M269 and are purely for comparison for those interested
- The first is a direct translation of the recursive Python version
- ► The second is derived from http://rosettacode.org/wiki/Binary\_search and is more idiomatic Haskell
- ► The code for both implementations is in the file M269BinarySearch.hs (which should be near the file of these slides)

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#### Haskell Example

Binary Search — Haskell — version 1 Binary Search — Haskell — version 2

Binary Search — Haskell — Comparison

Binary Search — Haskell — 1 (a)

module M269BinarySearch where

import Data.Array
import Data.List

- ► A Haskell script starts with a module header which starts with the reserved identifier, module followed by the module name, M269BinarySearch
- ► The module name must start with an upper case letter and is the same as the file name (without its extension of .hs or .lhs)
- Haskell uses layout (or the off-side rule) to determine scope of definitions, similar to Python
- ► The body of the module follows the reserved identifier where and starts with import declarations
- ► This imports the libraries Data.List, Data.Array

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- version 1

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Haskell Example
Binary Search — Haskell

Binary Search — Haskell — version 2 Binary Search — Haskell

ComparisonReferences

Binary Search — Haskell — 1 (b)

```
binarySearch :: Ord a => [a] -> a -> Maybe Int

binarySearch xs val

binarySearch01 xs val (lo,hi)

where

lo = 0

hi = length xs - 1
```

- Line 8 is the definition of binarySearch
- ► The preceding line, 6, is the type signature
- ▶ binarySearch takes a list and a value of type a (in the class Ord for ordering) and returns a Maybe Int a is a type variable
- ► The Maybe a type is an algebraic data type which is the union of the data constructors Nothing and Just a

```
data Maybe a = Nothing | Just a
```

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Haskell Example
Binary Search — Haskell

- version 1

Binary Search - Haskell
- version 2

Binary Search - Haskell

— Comparison

#### Code Description 1

- f:: t is a type signature for variable f that reads f is of type t
- f :: t1 -> t2 means that f has the type of a function that takes elements of type t1 and returns elements of type t2
- The function type arrow -> associates to the right

```
▶ f :: t1 -> t2 -> t3 means
▶ f :: t1 -> (t2 -> t3)
```

- ▶ f x function application is denoted by juxtaposition and is more binding than (almost) any other operation.
- Function application is left associative

```
► f x y means
```

▶ (f x) v

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Haskell Example Binary Search - Haskell

- version 1 Binary Search - Haskell

- version 2 Binary Search - Haskell

- Comparison References

Binary Search — Haskell — 1 (c)

```
binarvSearch01 :: Ord a
14
      => [a] -> a -> (Int, Int) -> Maybe Int
15
    binarySearch01 xs val (lo.hi)
17
      = if hi < lo then Nothing
18
        else
19
          let mid = (lo + hi) 'div' 2
20
21
              quess = xs !! mid
          in
22
          if val == guess
23
            then Just mid
24
          else if val < quess
25
            then binarySearch01 xs val (lo,mid-1)
26
          else
                 binarySearch01 xs val (mid + 1, hi)
27
```

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Binary Search — Haskell — version 1

- version 1

Binary Search — Haskell

version 2

Binary Search — Haskell

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Code Description 2

► A let expression has the form

**let** decls in expr

- dec1s is a number of declarations
- expr is an expression (which is the scope of the declarations)
- div is the integer division function
- In `div`, the grave accents (`) make a function into an infix operator (OK, that is syntactic sugar I need not have introduced and my formatting program has coerced the grave accent to a left single quotation mark Unicode U+2018, not the grave accent U+0060)
- ▶ (!!) is the list index operator first item has index 0

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Binary Search — Haskell

- version 1

Binary Search - Haskell
- version 2

Binary Search - Haskell

— Comparison

Binary Search — Haskell — 2 (a)

```
binarySearchGen :: Integral a
29
      \Rightarrow (a \Rightarrow Ordering) \Rightarrow (a, a) \Rightarrow Maybe a
30
    binarySearchGen p (lo,hi)
31
        hi < lo = Nothing
32
       | otherwise =
33
           let mid = (lo + hi) 'div' 2 in
34
           case p mid of
35
36
              LT -> binarySearchGen p (lo, mid - 1)
             GT -> binarySearchGen p (mid + 1, hi)
37
             EO -> Just mid
38
```

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Code Description 3

► A case expression has the form

case expr of alts

**expr** is evaluated and whichever alternative of **a1ts** matches is the result

- ► The lines starting with (|) are *guarded* definitions if the boolean expression to the right is True then the following expression is used
- otherwise is a synonym for True
- A conditional expression has the form

if expr then expr else expr

The first *expr* must be of type Bool

Guards and conditionals are alternative styles in programming

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Binary Search — Haskell — 2 (b)

```
binarySearchArray :: (Ix i. Integral i. Ord a)
40
                         => Array i a -> a -> Maybe i
41
    binarySearchArray ary x
42
      = binarySearchGen p (bounds arv)
43
        where
44
        p m = x 'compare' (arv ! m)
45
47
    binarySearchList :: Ord a
                      => [a] -> a -> Maybe Int
48
    binarySearchList xs val
49
         binarySearchGen p (0, length xs - 1)
50
         where
51
         p m = val 'compare' (xs !! m)
52
```

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#### Code Description 4

compare is a method of the Ord class, for ordering, defined in the standard Prelude

- Minimal type-specific definitions required are compare or (==) and (<=)</p>
- ! and !! are the array and list indexing operators

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► The first version with binarySearch and binarySearch01 is very similar to the *Python* recursive version binarySearchRec

- In the Haskell case an explicit helper function is used
- The second version is more general: binarySearchGen can be used with any type that is indexed by a data type in the Integral class
- binarySearchArray and binarySearchList specialise the function to arrays or lists.
- ► For the Haskell Array data type see the Haskell Report
- ► Idiomatic Haskell tends to be more general and make use of higher order functions, type classes and advanced features.

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### Web Links & References

#### Python IDEs

- Python Online IDEs
  - Repl.it https://repl.it/languages/python3 (Read-eval-print loop)
  - TutorialsPoint CodingGround Python 3 https://www.tutorialspoint.com/execute\_python3\_online.php
  - ► TutorialsPoint CodingGround Haskell ghci https://www.tutorialspoint.com/compile\_ haskell\_online.php

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### Web Links & References

#### References

► The offside rule (using layout to determine the start and end of code blocks) comes originally from Landin (1966) — see Off-side rule for other programming languages that use this.

- ► The *step-by-step* approach to writing programs is described in Glaser (2000)
- ► The difficulty in learning programs is described in many articles see, for example, Dehnadi (2006)
- Inductive data type
  - Algebraic data type composite type possibly recursive sum type of product types — common in modern functional languages.
  - Recursive data type from Type theory

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